

## New Leptoquark Mechanism of Neutrinoless Double Beta Decay

M. Hirsch, H.V. Klapdor-Kleingrothaus and S.G. Kovalenko\*

*Max-Planck-Institut für Kernphysik, P.O. 10 39 80, D-69029, Heidelberg,  
Germany*

*\*Joint Institute for Nuclear Research, Dubna, Russia*

### Abstract

A new mechanism for neutrinoless double beta ( $0\nu\beta\beta$ ) decay based on leptoquark exchange is discussed. Due to the specific helicity structure of the effective four-fermion interaction this contribution is strongly enhanced compared to the well-known mass mechanism of  $0\nu\beta\beta$  decay. As a result the corresponding leptoquark parameters are severely constrained from non-observation of  $0\nu\beta\beta$ -decay. These constraints are more stringent than those derived from other experiments.

*PACs:* 11.30, 12.30, 13.15, 14.80, 23.40

Neutrinoless double beta decay ( $0\nu\beta\beta$ ) is forbidden in the standard model (SM) of electro-weak interactions since it violates lepton number conservation. Therefore, experimental observation of this exotic process would be an unambiguous signal of physics beyond the SM (see refs. [1]-[4] for reviews).

Essential progress in the exploration of  $0\nu\beta\beta$ -decay both from theoretical and experimental sides has been achieved in the last few years (see, for instance [4] and references therein). The considerably improved experimental lower bounds on the half lives of various isotopes enhance the potential of  $0\nu\beta\beta$  experiments in testing different concepts of physics beyond the SM such as supersymmetry (SUSY) and leptoquarks (LQ).

The SUSY mechanisms of  $0\nu\beta\beta$ -decay were comprehensively investigated in a series of papers [5]-[9]. It turned out that constraints on certain SUSY-parameters from non-observation of  $0\nu\beta\beta$ -decay [7] are stronger than those from current and near future accelerator and non-accelerator experiments. Therefore, it is useful to investigate other possible contributions of physics beyond the SM to  $0\nu\beta\beta$ -decay to obtain  $0\nu\beta\beta$  constraints on the corresponding parameters.

In this note we present a new mechanism of  $0\nu\beta\beta$ -decay associated with the leptoquark contribution to the effective low-energy charged current lepton-quark interactions. The diagrams describing this contribution are presented in fig. 1.

The SM symmetries allow 5 scalar ( $S$ ) and 5 vector ( $V^\mu$ ) LQs with the following  $LQ(SU(3)_c \otimes SU(2)_L \otimes U(1)_Y)$  assignments:  $S_0(\bar{3}_c, 1; -2/3)$ ,  $\tilde{S}_0(\bar{3}_c, 1; -8/3)$ ,  $S_{1/2}(\bar{3}_c, 2; -7/3)$ ,  $\tilde{S}_{1/2}(\bar{3}_c, 2; -1/3)$ ,  $S_1(\bar{3}_c, 3; -2/3)$ ,  $V_0(\bar{3}_c, 1; -4/3)$ ,  $\tilde{V}_0(\bar{3}_c, 1; -10/3)$ ,  $V_{1/2}(\bar{3}_c, 2; -5/3)$ ,  $\tilde{V}_{1/2}(\bar{3}_c, 2; 1/3)$ ,  $V_1(\bar{3}_c, 3; -4/3)$ , where  $Y = 2(Q_{em} - T_3)$ .

The most general form of the renormalizable LQ-quark-lepton interactions consistent with  $SU(3)_c \otimes SU(2)_L \otimes U(1)_Y$  gauge symmetry can be written as [10]

$$\begin{aligned}
\mathcal{L}_{LQ-l-q} = & \lambda_{S_0}^{(R)} \cdot \overline{u_R^c} e_R \cdot S_0^{R\dagger} + \lambda_{\tilde{S}_0}^{(R)} \cdot \overline{d_R^c} e_R \cdot \tilde{S}_0^\dagger + \lambda_{S_{1/2}}^{(R)} \cdot \overline{u_R} \ell_L \cdot S_{1/2}^{R\dagger} + \\
& + \lambda_{\tilde{S}_{1/2}}^{(R)} \cdot \overline{d_R} \ell_L \cdot \tilde{S}_{1/2}^\dagger + \lambda_{S_0}^{(L)} \cdot \overline{q_L^c} i\tau_2 \ell_L \cdot S_0^{L\dagger} + \lambda_{S_{1/2}}^{(L)} \cdot \overline{q_L} i\tau_2 e_R \cdot S_{1/2}^{L\dagger} + \\
& + \lambda_{S_1}^{(L)} \cdot \overline{q_L^c} i\tau_2 \hat{S}_1^\dagger \ell_L + \lambda_{V_0}^{(R)} \cdot \overline{d_R} \gamma^\mu e_R \cdot V_{0\mu}^{R\dagger} + \lambda_{\tilde{V}_0}^{(R)} \cdot \overline{u_R} \gamma^\mu e_R \cdot \tilde{V}_{0\mu}^\dagger + \quad (1) \\
& + \lambda_{V_{1/2}}^{(R)} \cdot \overline{d_R^c} \gamma^\mu \ell_L \cdot V_{1/2\mu}^{R\dagger} + \lambda_{\tilde{V}_{1/2}}^{(R)} \cdot \overline{u_R^c} \gamma^\mu \ell_L \cdot \tilde{V}_{1/2\mu}^\dagger + \lambda_{V_0}^{(L)} \cdot \overline{q_L} \gamma^\mu \ell_L \cdot V_{0\mu}^{L\dagger} + \\
& + \lambda_{V_{1/2}}^{(L)} \cdot \overline{q_L^c} \gamma^\mu e_R \cdot V_{1/2\mu}^{L\dagger} + \lambda_{V_1}^{(L)} \cdot \overline{q_L} \gamma^\mu \hat{V}_{1\mu}^\dagger \ell_L + h.c.
\end{aligned}$$

Here  $q$  and  $\ell$  are the quark and the lepton doublets. Following [10, 11] we distinguish  $S(V)^{L,R}$  being LQs coupled to the left-handed and right-handed quarks respectively (see, however, the discussion on chiral couplings in [12]). For LQ triplets  $\Phi_1 = S_1, V_1^\mu$  the notation  $\hat{\Phi}_1 = \vec{\tau} \cdot \vec{\Phi}_1$  is used.

On the same footing the LQ fields couple to the SM Higgs doublet field  $H$ . A complete list of the renormalizable LQ-Higgs interactions is given in ref. [12]. These new interactions are especially important for  $0\nu\beta\beta$ -decay, since after electro-weak symmetry breaking they lead to mixing between different LQ multiplets. In turn this mixing generates the effective 4-fermion interactions involving right-handed leptonic currents. In combination with the ordinary SM left-handed charged current interactions the latter produce the contribution to  $0\nu\beta\beta$ -decay shown in the diagrams of fig. 1 with large enhancement factors. This type of contribution is absent in the case of decoupled LQ and Higgs sectors [12].

Under electro-weak symmetry breaking the neutral component of the SM Higgs field acquires a non-zero vacuum expectation value,  $\langle H^0 \rangle$ , which creates via LQ-Higgs interaction terms non-diagonal mass matrices for LQ fields with the same electric charge but from different  $SU(2)_L$  multiplets. To obtain observable predictions from the LQ-lepton-quark interaction Lagrangian in eq. (1), the LQ fields ( $I = S, V$ ) with non-diagonal mass matrices have to be rotated to the mass eigenstate basis  $I'$ . This can be done in the standard way:  $I(Q) = \mathcal{N}^{(I)}(Q) \cdot I'(Q)$ , where  $\mathcal{N}^{(I)}(Q)$  are orthogonal matrices such that

$\mathcal{N}^{(I)T}(Q_I) \cdot \mathcal{M}_I^2(Q) \cdot \mathcal{N}^{(I)}(Q) = \text{Diag}\{M_{I_n}^2\}$ , with the  $M_{I_n}$  being the mass of the relevant mass eigenstate field  $I'$ .

Now it is straightforward to derive the effective 4-fermion  $\nu - u - d - e$  interaction terms generated by the LQ exchange in the upper parts of the diagrams in fig. 1. After Fierz rearrangement they take the form [12]

$$\begin{aligned} \mathcal{L}_{LQ}^{eff} &= (\bar{\nu}P_R e^c) \left[ \frac{\epsilon_S}{M_S^2} (\bar{u}P_R d) + \frac{\epsilon_V}{M_V^2} (\bar{u}P_L d) \right] - \\ &- (\bar{\nu}\gamma^\mu P_L e^c) \\ &\times \left[ \left( \frac{\alpha_S^{(R)}}{M_S^2} + \frac{\alpha_V^{(R)}}{M_V^2} \right) (\bar{u}\gamma_\mu P_R d) - \sqrt{2} \left( \frac{\alpha_S^{(L)}}{M_S^2} + \frac{\alpha_V^{(L)}}{M_V^2} \right) (\bar{u}\gamma_\mu P_L d) \right], \end{aligned} \quad (2)$$

where

$$\epsilon_I = 2^{-\eta_I} \left[ \lambda_{I_1}^{(L)} \lambda_{I_{1/2}}^{(R)} \left( \theta_{43}^I(Q_I^{(1)}) + \eta_I \sqrt{2} \theta_{41}^I(Q_I^{(2)}) \right) - \lambda_{I_0}^{(L)} \lambda_{I_{1/2}}^{(R)} \theta_{13}^I(Q_I^{(1)}) \right] \quad (3)$$

$$\alpha_I^{(L)} = \frac{2}{3 + \eta_I} \lambda_{I_{1/2}}^{(L)} \lambda_{I_1}^{(L)} \theta_{24}^I(Q_I^{(2)}), \quad \alpha_I^{(R)} = \frac{2}{3 + \eta_I} \lambda_{I_0}^{(R)} \lambda_{I_{1/2}}^{(R)} \theta_{23}^I(Q_I^{(1)}). \quad (4)$$

$\eta_{S,V} = 1, -1$  for scalar and vector LQs.  $\theta_{kn}^I(Q)$  is a mixing parameter defined by

$$\theta_{kn}^I(Q) = \sum_l \mathcal{N}_{kl}^{(I)}(Q) \mathcal{N}_{nl}^{(I)}(Q) \left( \frac{M_I}{M_{I_l}(Q)} \right)^2, \quad (5)$$

where  $\mathcal{N}^{(I)}(Q)$  are mixing matrix elements for the scalar  $I = S$  and vector  $I = V$  LQ fields with electric charges  $Q = -1/3, -2/3$ . Common mass scales  $M_S$  of scalar and  $M_V$  of vector LQs are introduced for convenience.

Following the well known procedure [2] one can find the LQ contribution to the  $0\nu\beta\beta$ -decay matrix element for the diagrams in fig. 1. The LQ exchange sectors of these diagrams are described by the point-like 4-fermion interactions specified by the effective Lagrangian in eq. (2). Their bottom parts are the SM charged current interactions. The final formula for the inverse half-life of  $0\nu\beta\beta$ -decay reads

$$T_{1/2}^{-1}(0\nu\beta\beta) = |\mathcal{M}_{GT}|^2 \frac{2}{G_F^2} \left[ \tilde{C}_1 a^2 + C_4 b_R^2 + 2C_5 b_L^2 \right] \quad (6)$$

with

$$a = \frac{\epsilon_S}{M_S^2} + \frac{\epsilon_V}{M_V^2}, \quad b_{L,R} = \left( \frac{\alpha_S^{(L,R)}}{M_S^2} + \frac{\alpha_V^{(L,R)}}{M_V^2} \right), \quad \tilde{C}_1 = C_1 \left( \frac{\mathcal{M}_1^{(\nu)}}{M_{GT} - \alpha_2 M_F} \right)^2 \quad (7)$$

In eq. (6) the coefficients  $C_n$  are defined following [2];  $m_e$  and  $R$  are the electron mass and nuclear radius. We kept only the dominant terms in eq. (6), neglecting, particularly, terms proportional to the neutrino mass  $m_\nu$  which we assume to be very small and put  $m_\nu = 0$  in eq. (6). Also mixed terms, such as  $a \cdot b_{L/R}$ , are not accounted for, since these are expected to only slightly affect our numerical limits. The new matrix element  $\mathcal{M}_1^{(\nu)}$  was introduced and calculated in ref. [9] within the pn-QRPA framework. Calculating  $C_i$  within the same approach [13] for the particular case of  $^{76}\text{Ge}$  we have a complete set of nuclear structure coefficients in eq. (6) (all in units of inverse years):  $|\mathcal{M}_{GT}|^2 \tilde{C}_1 = 1.63 \times 10^{-10}$ ,  $|\mathcal{M}_{GT}|^2 C_4 = 1.36 \times 10^{-13}$ ,  $|\mathcal{M}_{GT}|^2 C_5 = 4.44 \times 10^{-9}$ .

Now we are ready to derive constraints on the LQ parameters  $a, b_{L,R}$  in eq. (6). We use the result from the Heidelberg-Moscow  $^{76}\text{Ge}$  experiment [14]  $T_{1/2}^{0\nu\beta\beta}(^{76}\text{Ge}, 0^+ \rightarrow 0^+) > 7.4 \times 10^{24} \text{ years } 90\% \text{ c.l.}$

Assuming no spurious cancellations between the different terms in eq. (6) we derive the following constraints on the effective LQ parameters:

$$\epsilon_I \leq 2.4 \times 10^{-9} \left( \frac{M_I}{100\text{GeV}} \right)^2, \quad (8)$$

$$\alpha_I^{(L)} \leq 2.3 \times 10^{-10} \left( \frac{M_I}{100\text{GeV}} \right)^2, \quad (9)$$

$$\alpha_I^{(R)} \leq 8.3 \times 10^{-8} \left( \frac{M_I}{100\text{GeV}} \right)^2. \quad (10)$$

Recall  $I = S, V$ .

It is interesting to compare these constraints with the corresponding constraints from other processes [11]. Consider the helicity-suppressed decay  $\pi \rightarrow e\nu$  which is extremely sensitive to the first two scalar-pseudoscalar terms in eq. (2), leading to a helicity-unsuppressed amplitude [11]. The following constraint from  $\pi \rightarrow e\nu$ -decay data was obtained in ref. [12]:  $\epsilon_I \leq 5 \times 10^{-7} (M_I/100\text{GeV})^2$ . Apparently, the corresponding constraints from  $0\nu\beta\beta$ -decay in eq. (8) are more stringent by about two orders of magnitude. This confirms that  $0\nu\beta\beta$ -decay is a powerful probe of physics beyond the standard model.

In summary, non-observation of  $0\nu\beta\beta$  decay can provide stringent bounds on parameters of extensions of the standard model. Moreover, the  $0\nu\beta\beta$  decay bounds on some of these fundamental parameters can be much more stringent than those from other experiments. Previously such a conclusion was obtained for the case of the R-parity violating supersymmetric contribution to  $0\nu\beta\beta$ -

decay [7]-[9]. In this letter we have shown that the leptoquark mechanism allows similar conclusions.

### ACKNOWLEDGMENTS

We thank V.A. Bednyakov, D.I. Kazakov for helpful discussions. M.H. would like to thank the Deutsche Forschungsgemeinschaft for financial support by grants kl 253/8-1 and 446 JAP-113/101/0.

### References

- [1] W.C. Haxton and G.J. Stephenson, *Progr. Part. Nucl. Phys.* 12 (1984) 409; K. Grotz and H.V. Klapdor-Kleingrothaus, *The Weak Interaction in Nuclear, Particle and Astrophysics*, Adam Hilger, Bristol, New York, 1990;  
R.N. Mohapatra and P.B. Pal, *Massive Neutrinos in Physics and Astrophysics*, World Scientific, Singapore, 1991; M. Moe and P. Vogel, *Annual Review of Nucl. and Part. Science* 44 (1994) 247.
- [2] M. Doi, T. Kotani and E. Takasugi, *Progr. Theor. Phys. Suppl.* 83 (1985) 1;
- [3] J. D. Vergados, *Phys. Report*, 133 (1986) 1; J.W.F. Valle, *Prog. Part. Nucl. Phys.* 26 (1991) 91.
- [4] *Proc. of the Int. Workshop on Double Beta Decay and Related Topics*, Trento, Italy, April 24-May 5, 1995, ed. by H.V. Klapdor-Kleingrothaus and S. Stoica, World Scientific, Singapore, 1996
- [5] R.N. Mohapatra, *Phys.Rev.* D34 (1986) 3457.
- [6] J.D Vergados, *Phys.Lett.* B184 (1987) 55.
- [7] M. Hirsch, H.V. Klapdor-Kleingrothaus and S.G. Kovalenko, *Phys.Lett.* B352 (1995) 1; *Phys. Rev. Lett.*, 75 (1995) 17; *Phys. Rev.* D53 (1996) 1329.
- [8] K.S. Babu and R.N. Mohapatra, *Phys.Rev.Lett.*, 75 (1995)2276;
- [9] M. Hirsch, H.V. Klapdor-Kleingrothaus and S.G. Kovalenko, hep-ph/9512237, to appear in *Phys. Lett. B* (1996).

- [10] W. Buchmüller, R. Rückl and D. Wyler, Phys.Lett. B191 (1987) 442.
- [11] S. Davidson, D. Bailey and A. Campbell, Z.Phys. C61 (1994) 613; M. Leurer, Phys.Rev.Lett. 71 (1993) 1324; Phys.Rev. D50 (1994) 536.
- [12] M. Hirsch, H.V. Klapdor-Kleingrothaus, S.G. Kovalenko, hep-ph/9602305 (submitted to Phys.Lett. B)
- [13] K. Muto, E. Bender and H.V. Klapdor, Z. Phys. A334 (1989) 177,187
- [14] HEIDELBERG-MOSCOW Collaboration: A. Balysh et al., Phys.Lett. B 356 (1995) 450.

### Figure Captions

Fig.1 Feynman graphs for the leptoquark-induced mechanism of  $0\nu\beta\beta$  decay.  $S$  and  $V^\mu$  stand symbolically for a)  $Q = -1/3$  (upper part) and b)  $Q = 2/3$  (lower part) scalar and vector LQs.

Figure 1

