The pulsations of the B5IVe star HD 181231 observed with CoRoT and ground-based spectroscopy*,**

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ABSTRACT

Context. HD 181231 is a B5IVe star, which has been observed with the CoRoT satellite during ~5 consecutive months and simultaneously from the ground in spectroscopy and spectropolarimetry.

Aims. By analysing these data, we aim to detect and characterize as many pulsation frequencies as possible, to search for the presence of beating effects possibly at the origin of the Be phenomenon. Our results will also provide a basis for seismic modelling.

Methods. The fundamental parameters of the star are determined from spectral fitting and from the study of the circumstellar emission. The CoRoT photometric data and ground-based spectroscopy are analysed using several Fourier techniques: CLEAN-NG, PASPER, and TISAFT, as well as a time-frequency technique. A search for a magnetic field is performed by applying the LSD technique to the spectropolarimetric data.

Results. We find that HD 181231 is a B5IVe star seen with an inclination of ~45 degrees. No magnetic field is detected in its photosphere. We detect at least 10 independent significant frequencies of variations among the 54 detected frequencies, interpreted in terms of non-radial pulsation modes and rotation. Two longer-term variations are also detected: one at ~14 days resulting from a beating effect between the two main frequencies of short-term variations, the other at ~116 days due either to a beating of frequencies or to a zonal pulsation mode.

Conclusions. Our analysis of the CoRoT light curve and ground-based spectroscopic data of HD 181231 has led to the determination of the fundamental and pulsational parameters of the star, including beating effects. This will allow a precise seismic modelling of this star.

Key words. stars: early-type – stars: emission-line, Be – stars: individual: HD 181231 – stars: rotation – stars: oscillations

1 Introduction

Be stars are main sequence or slightly evolved non-supergiant, late-O, B, or early-A stars that show or have shown at least once emission in their Balmer lines caused by the presence of a decretion circumstellar disk. Emission can also appear in other lines of the spectrum, in particular in red HeI lines or FeII lines. Moreover, the disk produces an infrared excess in the spectral energy distribution. In addition to this disk, Be stars also exhibit polar winds. About 20% of all B stars in our galaxy are Be stars. However, this fraction depends on metallicity (Martayan et al. 2006, 2007). Therefore, in other environments of lower metallicity, the fraction of Be stars over B stars can be much higher. Only B stars of sufficiently high rotational velocity at the ZAMS
Table 1. Log of the spectroscopic and spectropolarimetric observations.

<table>
<thead>
<tr>
<th>Instr.</th>
<th>Date</th>
<th>$T_{\text{exp}}$ (s)</th>
<th>#</th>
<th>Instr.</th>
<th>Date</th>
<th>$T_{\text{exp}}$ (s)</th>
<th>#</th>
</tr>
</thead>
<tbody>
<tr>
<td>BeSS</td>
<td>25.05.07</td>
<td>4500</td>
<td>1</td>
<td>FEROS</td>
<td>01.07.07</td>
<td>600–660</td>
<td>6</td>
</tr>
<tr>
<td>BeSS</td>
<td>03.06.07</td>
<td>5531</td>
<td>1</td>
<td>FEROS</td>
<td>02.07.07</td>
<td>510–770</td>
<td>6</td>
</tr>
<tr>
<td>BeSS</td>
<td>08.06.07</td>
<td>6900</td>
<td>1</td>
<td>Narval</td>
<td>02.07.07</td>
<td>4*900</td>
<td>2</td>
</tr>
<tr>
<td>BeSS</td>
<td>23.06.07</td>
<td>5430</td>
<td>1</td>
<td>FEROS</td>
<td>03.07.07</td>
<td>550–630</td>
<td>5</td>
</tr>
<tr>
<td>Narval</td>
<td>23.06.07</td>
<td>4*900</td>
<td>2</td>
<td>FEROS</td>
<td>04.07.07</td>
<td>630–750</td>
<td>4</td>
</tr>
<tr>
<td>FEROS</td>
<td>25.06.07</td>
<td>900</td>
<td>4</td>
<td>Narval</td>
<td>04.07.07</td>
<td>4*900</td>
<td>2</td>
</tr>
<tr>
<td>Narval</td>
<td>25.06.07</td>
<td>4*900</td>
<td>2</td>
<td>BeSS</td>
<td>07.07.07</td>
<td>1800</td>
<td>1</td>
</tr>
<tr>
<td>FEROS</td>
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<td>900</td>
<td>2</td>
<td>BeSS</td>
<td>12.07.07</td>
<td>7800</td>
<td>1</td>
</tr>
<tr>
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<td>26.06.07</td>
<td>4*900</td>
<td>2</td>
<td>BeSS</td>
<td>13.07.07</td>
<td>3618</td>
<td>1</td>
</tr>
<tr>
<td>FEROS</td>
<td>27.06.07</td>
<td>900</td>
<td>4</td>
<td>FEROS</td>
<td>16.07.07</td>
<td>900</td>
<td>6</td>
</tr>
<tr>
<td>Narval</td>
<td>27.06.07</td>
<td>4*900</td>
<td>2</td>
<td>FEROS</td>
<td>17.07.07</td>
<td>900</td>
<td>6</td>
</tr>
<tr>
<td>FEROS</td>
<td>28.06.07</td>
<td>550–870</td>
<td>5</td>
<td>FEROS</td>
<td>18.07.07</td>
<td>800–900</td>
<td>5</td>
</tr>
<tr>
<td>Narval</td>
<td>28.06.07</td>
<td>4*900</td>
<td>2</td>
<td>FEROS</td>
<td>19.07.07</td>
<td>700–900</td>
<td>5</td>
</tr>
<tr>
<td>FEROS</td>
<td>29.06.07</td>
<td>810–850</td>
<td>4</td>
<td>FEROS</td>
<td>20.07.07</td>
<td>600–900</td>
<td>4</td>
</tr>
<tr>
<td>Narval</td>
<td>29.06.07</td>
<td>4*900</td>
<td>2</td>
<td>BeSS</td>
<td>21.07.07</td>
<td>4222</td>
<td>1</td>
</tr>
<tr>
<td>FEROS</td>
<td>30.06.07</td>
<td>900</td>
<td>6</td>
<td>BeSS</td>
<td>10.10.07</td>
<td>4500</td>
<td>1</td>
</tr>
<tr>
<td>Narval</td>
<td>30.06.07</td>
<td>4*900</td>
<td>2</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

The origin of the spectra, date, exposure time, and number of spectra acquired on that date are provided.

No longitudinal magnetic field is detected down to a level of $\sim 650$ G. Using an inclination angle of $i = 45$ degrees, this corresponds to a maximum oblique dipole effective field of $B_{\text{eff}} = 3200$ G.

2. Observations

The star HD 181231 was observed with the CoRoT satellite for $\sim 5$ consecutive months. Ground-based observations were simultaneously obtained for about three weeks in terms of spectroscopy with FEROS mounted on the ESO 2.2 m telescope and in terms of spectropolarimetry with Narval mounted on the TBL (Pic du Midi, France). Additional spectra from the BeSS database were also collected. A log of the observations is provided in Table 1.

2.1. CoRoT photometric observations

CoRoT was launched on December 27, 2006. The raw photometric data acquired with CoRoT were reduced by the CoRoT team. The corrections applied to the data were the subtraction of the offset and background, the correction for the cross-talk effect, the transformation from ADU to electrons, the corrections of the exposure time variations, jitter effect, and outliers. For more details, we refer to Auvergne et al. (2009) and Samadi et al. (2006).

In the asteroseismology field, CoRoT obtains one measurement every second. Averaged measurements every 32 s are then calculated and constitute the light curve, with time converted to the heliocentric system. A flag is assigned to each datapoint to indicate if this measurement has been obtained during a proton impact, the South Atlantic Anomaly (SAA) crossing, a transition of the satellite from light to penumbra or vice versa, a large jitter correction, or a light-curve discontinuity because of temperature effects.

In this paper, we analysed both the light curve with only datapoints with flag 0, i.e., taken in perfect conditions, which corresponds to 377 298 photometric measurements, and the light curve for which the 45 059 points with non-0 flag have been replaced by interpolated points or uncorrected.

HD 181231 was observed by CoRoT during its LRC1 long run. The observations lasted 156.64 days from May 11 to October 15, 2007, and were uninterrupted. The CoRoT light curve (Fig. 1) was detrended with a linear fit to remove the linear effect of ageing of some instrument parts (CCDs and/or optics). The light curve shows variations with a maximum peak-to-peak amplitude of 11 millimag (see top panel of Fig. 1) and a peak-to-peak point scatter due to noise of less than 0.8 millimag. The noise level of the CoRoT data for HD 181231 is about 3 ppm in 5 days, i.e., very close to the photon noise of 2 ppm. The difference is caused by a jitter correction residue.

2.2. FEROS spectroscopic observations

HD 181231 was observed from June 26 to July 21, 2007, at ESO/La Silla with the FEROS spectrograph attached to the 2.2 m telescope. Unfortunately, the dates of our FEROS observations coincide with the minimum amplitude of variations in the CoRoT light curve (see Figs. 1 and 6).

A total of 72 échelle spectra were obtained with exposure times of between 510 and 900 s and a signal to noise of 140 to 250. The spectral resolution is 48 000 and the wavelength ranges from 3500 to 9200 Å on 39 échelle orders. This observing time was awarded in the framework of an ESO Large Programme.
The Narval observations were collected at the same time as the FEROS observations, i.e., at the minimum amplitude of variations in the CoRoT light curve (see Figs. 1 and 6). The Narval observations were collected at the same time as the FEROS observations, i.e., at the minimum amplitude of variations in the CoRoT light curve (see Figs. 1 and 6).

2.3. Narval spectropolarimetric observations

A set of spectropolarimetric observations was obtained with Narval mounted on the 2-m Télescope Bernard Lyot (TBL) at Pic du Midi (France) from June 23 to July 4, 2007 (PI: Catala). The Narval observations were collected at the same time as the FEROS observations, i.e., at the minimum amplitude of variations in the CoRoT light curve (see Figs. 1 and 6).

Eighteen échelle spectra were acquired with signal-to-noise ratio of between 110 and 190. The spectral resolution is 65 000 and the wavelength ranges from 3690 and 10 480 Å. They have been obtained in spectropolarimetric mode in Stokes V spectra are used in the search for a magnetic field.

Table 2. Apparent value of the stellar parameters of HD 181231.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>F06</th>
<th>This work</th>
</tr>
</thead>
<tbody>
<tr>
<td>$T_{\text{eff}}$ (K)</td>
<td>14 000 ± 1000</td>
<td>13 700 ± 1500</td>
</tr>
<tr>
<td>log $g$</td>
<td>3.73 ± 0.10</td>
<td>3.47 ± 0.20</td>
</tr>
<tr>
<td>$v \sin i$ spectral fit (km s$^{-1}$)</td>
<td>250 ± 30</td>
<td>175 ± 25</td>
</tr>
<tr>
<td>$v \sin i$ Fourier (km s$^{-1}$)</td>
<td>165 ± 30</td>
<td>165 ± 30</td>
</tr>
</tbody>
</table>

2.4. BeSS spectra

Nine H$\alpha$ spectra obtained during the CoRoT run by amateur astronomers were retrieved from the BeSS database and are used in this study as an indication of the emission level and variability of the star. All these spectra were collected with the Cassegrain spectrograph mounted on the Boller & Chivens telescope in Brazil with a resolution of ∼7000 and a signal-to-noise ratio of 80. The parameters found in F06 are reported in Table 2.

By analysing the new spectra acquired for this work, which are of both higher spectral resolution and higher signal-to-noise ratio, we can re-determine the parameters with a higher confidence level. We used an average of the 72 FEROS spectra. The new data clearly show that, in spite of the low effective temperature, the spectrum of HD 181231 exhibits a large number of small emission features superimposed on photospheric lines that mainly belong to H$\alpha$, Fe II, Si II, C II, and Mg II. The presence of these features (invisible in the lower resolution 2006 data) makes the continuum normalization and the interpretation of the spectrum far more complex than assumed in F06.

In Fig. 2, we compare the 2006 data (black) of F06 with the new data (red) that we convolved with an average of the 72 FEROS spectra. The new data clearly show that, in spite of the low effective temperature, the spectrum of HD 181231 exhibits a large number of small emission features superimposed on photospheric lines that mainly belong to H$\alpha$, Fe II, Si II, C II, and Mg II. The presence of these features (invisible in the lower resolution 2006 data) makes the continuum normalization and the interpretation of the spectrum far more complex than assumed in F06.

3. The star HD 181231

3.1. Fundamental parameters

HD 181231 is a B5IVe star (Frémat et al. 2006, hereafter F06) of magnitude $V = 8.58$. According to the Hipparcos catalogue (Perryman et al. 1997), it is situated at 3.36 kpc, but at only 590 pc, according to Kozok (1985).

In F06, we determined the fundamental parameters of HD181231 from one spectrum extracted from the GAUDI database, obtained with the Cassegrain spectrograph mounted on the Boller & Chivens telescope in Brazil with a resolution of ~7000 and a signal-to-noise ratio of 80. The parameters found in F06 are reported in Table 2.

3.2. Binary parameters

HD 181231 is a binary system with an orbital period of 14.1 days. The orbit has a high inclination, with the projected rotation velocity ($v \sin i$) of the primary being determined from high-resolution spectroscopy and the radial velocities of the secondary star are available from the BeSS database.

The effective temperature ($T_{\text{eff}}$), surface gravity (log $g$), and projected rotation velocity ($v \sin i$) are derived from the average FEROS spectrum using the procedure described in F06. We assume a solar metallicity. Our main fitting criteria are the neutral helium lines and the wings of the H$\alpha$ line, which exhibits a weaker emission core. The wavelength range 4400–4450 Å is ignored in the fitting procedure because of the presence of an unknown feature (Kozok 1985).

1 http://basebe.obspm.fr
2 Shelyak Instruments, http://www.shelyak.com
interstellar band at 4425 Å. The average value of the parameters that we obtained are given in Table 2, with their uncertainties.

Error bars were estimated by performing multiple fits, selecting different lines and fixing one parameter ($T_{\text{eff}}$ or $\log g$) at a time, while allowing the others to vary. The range of parameters that provide acceptable agreement with the observations infer the accuracy of the parameters (see e.g., Fig. 3).

For comparison, we also determined $v \sin i$ by computing the Fourier transform (see e.g., Royer et al. 2002) of the CI 4267 line profile (Fig. 4). This line was chosen because it appears to be unaffected by emission. The result is given in Table 2 and is coherent with that found by fitting the helium line profiles.

Assuming that $\Omega$ (where $\Omega$ and $\Omega_c$ are the angular velocity and its critical value, respectively) ranges from 0.8 to 0.99, we corrected the stellar parameters for gravitational darkening effects following F06 and using corrections computed in Frémat et al. (2005) to obtain an estimate of the stellar parameters of the non-rotating counterpart of the star as well as its true $v \sin i$ value. The results are listed in Table 3. We find in particular that the rotation frequency is $f_{\text{rot}} = 0.75 \pm 0.32 \text{ c d}^{-1}$.

3.2. Disk emission

The Hα, Hβ, and Hγ lines exhibit strong emission in the profiles and Hδ shows an inverted winebottle shape. Following the atlas of Hanuschik et al. (1996), we classify the star on the basis of its Hα and Fe II 5316 line profiles and estimate the disk inclination.

The average profiles of the Hα, Hβ, and Fe II 5316 lines are displayed in Fig. 5. The line profiles exhibit two symmetrical emission peaks (class 1) with weak winebottle shoulders and Hα even exhibits a third peak in its red wing. Therefore, the star may be classified as L1 (inclinations of between 10 and 60 degrees) in the Hanuschik atlas. This is compatible with the value derived above from the spectral fitting of fundamental parameters (Table 3). We note, that the V-shaped central depression of the Fe II 5169 and 5316 profiles implies that the star should rather be classified as H1 (inclinations between 60 and 80 degrees). However, these lines are much less reliable for a disk classification.

Following Eq. (7) in Hummel & Vrancken (1995), we determine the radius of the circumstellar disk from the distance between the averaged V and R peaks of Hα. We find that $R_\text{D} = (2 \times 169/92.3)^2 = 13.4 \text{ R}_\odot$.

The intensity of the emission in Hα compared to the continuum level, observed in the spectra retrieved from the BeSS database and obtained with FEROS and Narval during the CoRoT run, is plotted in Fig. 6. The BeSS datapoints exhibit a scatter caused by the lower signal-to-noise ratio of these spectra obtained with small telescopes. Intrinsic variations are, however, clearly observed in the FEROS and Narval data with an estimated period of ~15 days. The V, R, and V/R quantities measured in the Hα line also exhibit variations but no clear periodicity.

3.3. Variability

Although HD 181231 is classified as constant in the Hipparcos catalogue (Perryman et al. 1997), it was re-classified instead as variable on the basis of ground-based spectroscopic observations with a frequency of 0.67 c d$^{-1}$ (Gutiérrez-Soto et al. 2007).

3.4. Magnetic field

We analysed the spectropolarimetric Stokes V data obtained with Narval to search for the presence of a magnetic field. We
The final list contains 139 lines. Of these, 126 lines were contaminated by circumstellar emission and lines invisible in the spectrum of HD 181231. The remaining 13 lines infer values compatible with 0 with typical error bars of the order of 650 G. We thus find no evidence of a magnetic field in this star at the detection level we reached, i.e., we can define an upper limit to $B_{\text{long}}$ equal to $\sim 650$ G in our observations.

The error bars in $T_{\text{eff}}$ are $\pm 1500$ K, in $\log g \pm 0.20$, in $v \sin i \pm 25$ km s$^{-1}$ and in $\log L/L_\odot \pm 0.5$.

The 3 methods were applied to the CoRoT light curve with CoRoT Be team. TISAFT uses a statistical Fisher test to decide which of the peaks in the power spectrum correspond to significant signal. CLEAN-NG uses a stopping criterion based on the relative rate $r$ of increase in the total power in the clean components from one iteration to the next one. We used $r = 0.0001$ and an oversampling of 16. We note that PASPER collects peaks of highest amplitudes until it finds one peak that does not fulfil the empirical criterion $S/N > 4$. Since the noise decreases with frequency, it can thus miss peaks at high frequencies with $S/N > 4$ but low amplitudes. For a detailed description of these methods, we refer to Gutiérrez-Soto et al. (2009).

Frequencies found with these 3 methods, their amplitude and phase, as well as the interpretation of each frequency in terms of stellar signal or combinations, but excluding instrumental frequencies such as the orbital frequency of the satellite, are given in Table 5. The amplitudes and phases, and their errors, obtained for each set of frequencies with these three methods were recalculated with AMPHI to achieve greater accuracy and homogeneity and are also given in Table 5. For a complete set of fixed frequencies, this program calculates the amplitudes and phases to obtain the best fit to the light curve (see Gutiérrez-Soto et al. 2009).

The 3 methods were applied to the CoRoT light curve with both gaps and interpolated points (see Sect. 2) and yielded frequencies found with these 3 methods, their amplitude and phase, as well as the interpretation of each frequency in terms of stellar signal or combinations, but excluding instrumental frequencies such as the orbital frequency of the satellite, are given in Table 5. The amplitudes and phases, and their errors, obtained for each set of frequencies with these three methods were recalculated with AMPHI to achieve greater accuracy and homogeneity and are also given in Table 5. For a complete set of fixed frequencies, this program calculates the amplitudes and phases to obtain the best fit to the light curve (see Gutiérrez-Soto et al. 2009).

Fig. 6. Variation in the emission intensity in the H$\alpha$ line as observed during the CoRoT run with the FEROS and Narval spectrographs and by amateur astronomers C. Buil, J. Ribeiro, and O. Thizy as a contribution to the BeSS database.

4. Time-series analysis

4.1. CoRoT photometric data

CoRoT data were analysed using several Fourier techniques: CLEAN-NG, PASPER, and TISAFT, all developed within the CoRoT Be team. TISAFT uses a statistical Fisher test to decide which of the peaks in the power spectrum correspond to significant signal. CLEAN-NG uses a stopping criterion based on the relative rate $r$ of increase in the total power in the clean components from one iteration to the next one. We used $r = 0.0001$ and an oversampling of 16. We note that PASPER collects peaks of highest amplitudes until it finds one peak that does not fulfil the empirical criterion $S/N > 4$. Since the noise decreases with frequency, it can thus miss peaks at high frequencies with $S/N > 4$ but low amplitudes. For a detailed description of these methods, we refer to Gutiérrez-Soto et al. (2009).

Fig. 5. Averaged line profiles of the H$\alpha$, H$\beta$, and Fe II 5316 lines from FEROS data.

Table 3. Parameters corrected for gravitational darkening effects at different $T_{\text{eff}}$ values.

<table>
<thead>
<tr>
<th>$T_{\text{eff}}$ (K)</th>
<th>$\log g$</th>
<th>$v \sin i$ (km s$^{-1}$)</th>
<th>$i$ (deg)</th>
<th>$R_{\odot}$ (R$_\odot$)</th>
<th>$f_{\odot}$ (c d$^{-1}$)</th>
<th>$M$ (M$_\odot$)</th>
<th>$\log L/L_\odot$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.80</td>
<td>14 300</td>
<td>3.62</td>
<td>178</td>
<td>49 ± 10</td>
<td>6.5 ± 2.5</td>
<td>0.72 ± 0.32</td>
<td>4.4 ± 1.3</td>
</tr>
<tr>
<td>0.90</td>
<td>14 300</td>
<td>3.59</td>
<td>191</td>
<td>44 ± 7</td>
<td>7.2 ± 2.8</td>
<td>0.76 ± 0.33</td>
<td>4.4 ± 1.3</td>
</tr>
<tr>
<td>0.95</td>
<td>14 200</td>
<td>3.57</td>
<td>195</td>
<td>40 ± 6</td>
<td>7.8 ± 2.9</td>
<td>0.78 ± 0.31</td>
<td>4.5 ± 1.4</td>
</tr>
<tr>
<td>0.99</td>
<td>14 000</td>
<td>3.51</td>
<td>210</td>
<td>40 ± 6</td>
<td>8.9 ± 3.4</td>
<td>0.73 ± 0.31</td>
<td>4.5 ± 1.4</td>
</tr>
</tbody>
</table>

The 3 methods were applied to the CoRoT light curve with both gaps and interpolated points (see Sect. 2) and yielded...
similar results. The interpolation, however, allows us to easily suppress peaks produced by the observing window (see Gutiérrez-Soto et al. 2009). The minimum detectable frequency is $1/T = 0.0064 \, \text{c d}^{-1}$, i.e., $0.075 \, \mu\text{Hz}$, where $T$ is the length of the run. Following Kallinger et al. (2008), the frequency uncertainty of close peaks is $\Delta f = 1/(4T) = 0.0016 \, \text{c d}^{-1}$, i.e., $0.019 \, \mu\text{Hz}$. A power spectrum of all significant frequencies obtained with the three methods is shown in Fig. 7.

The main frequencies were found with all three methods. We note however that TISAFT detects a frequency at $0.6284 \, \text{c d}^{-1}$ that differs slightly from the one at $0.624 \, \text{c d}^{-1}$ obtained with the other two methods, and of lower amplitude. In the case of CLEAN-NG, the frequency at $0.624 \, \text{c d}^{-1}$ is divided into two close peaks and the sum of the two amplitudes (1.372 mmag) should be considered as the amplitude for this frequency.

Moreover, TISAFT detects several frequencies between 0.1 and $0.4 \, \text{c d}^{-1}$, which the other two methods do not detect. These frequencies could be related to the sync function of the low frequencies and should be considered with care.

A plot of the CoRoT light curve folded in phase with the two detected frequencies of the highest amplitudes ($f_1 = 0.695 \, \text{c d}^{-1}$ and $f_2 = 0.624 \, \text{c d}^{-1}$) is shown in Fig. 8. A phase-binned curve and a sinusoidal fit are superimposed in each panel. A similar analysis with a method based on the Morlet wavelet (Baudin et al. 1994, 1996) was performed (see Fig. 11). The Morlet wavelet provides a superior trade-off between frequency resolution and time resolution than the above method. Nevertheless, it yields similar results.

4.2. Ground-based spectroscopic data

A time series analysis is performed using Fourier Transform and least squares fitting methods, as in Floquet et al. (2002) and Neiner et al. (2005) with the FEROS data. These methods are applied to each wavelength bin of the line-profile time series to study the line profile variations (lpv) of the HeI 4026, 4143, 4387, 4471, 4713, 4922, 6678, MgII 4481, SiII 4128, 4130, 5056, CII 4267, Hα and Hβ lines. The minimum detectable frequency is $1/T = 0.04 \, \text{c d}^{-1}$, i.e., $0.46 \, \mu\text{Hz}$, where $T$ is the length of the FEROS run. The error bar of the frequencies is $\Delta f = 1/(4T) = 0.01 \, \text{c d}^{-1}$, i.e., $0.12 \, \mu\text{Hz}$.

The frequency $0.69 \, \text{c d}^{-1}$ is detected in the lpv of the MgII 4481 and HeI 4471 lines. This frequency corresponds to $f_1$ detected in the CoRoT data. The power and phase distributions of this frequency are displayed in Fig. 10 for the two lines. We note that the power is higher in the wings than in the centre of the lines. In terms of non-radial pulsations, an initial guess of the pulsation parameters can be obtained from the Intensity Period Search method (Telting & Schrijvers 1997). The blue-to-red phase difference found for a frequency is an indicator of the typical degree $\ell$. From the phase difference of the variations with

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**Fig. 7.** Power spectrum of all significant frequencies detected by TISAFT, CLEAN-NG, and PASPER. A zoom at the main frequencies is shown in the top right panel, with the same axis as in the main panel.

**Fig. 8.** CoRoT light curve folded with the two main frequencies detected. A phase-binned curve (red) and a sinusoidal fit (blue) as a single (for $f_1$) or double wave (for $f_2$) are superimposed in each panel.
the frequency $0.69 \, \text{c/d}$ ($\Delta \phi \sim 3$), we thus estimate the $\ell$-degree of the mode to be $\sim 3$.

We note that the spectra are contaminated with Fe II lines in emission, because of the circumstellar disk. This is probably why we only find a coherent phase in the Mg II 4481 and He I 4471 lines for $f = 0.69 \, \text{c/d}^{-1}$. Greyscale dynamical spectra of the Mg II 4481 and He I 4471 lines folded in phase with the frequency $0.69 \, \text{c/d}$ were calculated. However, they do not show any clear pattern.

Other detected frequencies for the FEROS data, given in Table 4, have incoherent phase distributions. Most of them are probably pseudo-periods or artifacts in the observations. We note however that a frequency at $\sim 1.25 \, \text{c/d}$ is detected in the He I 4143, C II 4267, and H$\beta$ lines, which corresponds to the harmonics $2^* f/2$ detected in the CoRoT data. A frequency at $0.64 \, \text{c/d}$, i.e., close to $f/2$, is also detected in the He I 4922 line.

The radial velocity (RV) of the line centroid, the central depth (CD), the full-width at half-maximum (FWHM), and the equivalent width (EW) of some of the lines are also studied in detail for each line profile with the standard Fourier techniques. A non-linear multi-parameter fitting code (Vaníček 1971) was used to search for frequencies in these spectral parameters. We found again the frequency $0.69 \, \text{c/d}$ in the variations of the RV, CD, and FWHM of the Mg II 4481, and in the RV and CD of the He I 4471 lines. Twice this frequency, $1.38 \, \text{c/d}$, is detected in the EW of the He I 4471 line. A clear frequency is detected in neither the other line quantities of these two lines, nor the He I 4387 line.

The phase diagram with $f_1 = 0.695 \, \text{c/d}$ for the EW of the Mg II 4481 line is shown in Fig. 12. The binned and scaled CoRoT light curve folded with this frequency has been superimposed. We note that the radial velocity maximum occurs about a quarter of a period ($\Delta \Phi = 0.28$) after maximum light.

The small number of Narval spectra does not allow us to perform a complete analysis of the lpv or spectral quantities for those data. Nevertheless, a frequency at $0.67 \, \text{c/d}$ was detected in the lpv for the Mg II 4481 and He I 4471 lines, but with no coherent phase diagram, probably because of the uncertainty in the determination of the sinusoidal function. However, the detected frequency is consistent with the frequency at $0.69 \, \text{c/d}$ detected in the FEROS data.
5. Discussion

In the following sections, we discuss the results obtained in this work for the Be star HD 181231 in the light of pulsations, rotation, and beating effects.

5.1. Pulsations and rotation

We have detected at least 10 significant independent frequencies of variations in the CoRoT light curve of HD 181231. This number of detected frequencies may seem small compared to the e.g., ∼60 frequencies detected for HD 163868 using a few weeks of MOST observations (Walker et al. 2005), while we have observed HD 181231 during 5 months. However, we have cleaned our list of 54 detected frequencies from all combination frequencies and harmonics. Therefore, we consider here only independent true stellar frequencies. We note in addition that, in hot stars, each detected frequency provides information about a different layer of the star. Therefore, seismic modelling can be very powerful for those objects even when only a few frequencies are detected.

The frequency peak with the second highest amplitude (1.3 mmag) is detected at $f_1 = 0.695 \, \text{c d}^{-1}$ (7.22 $\mu$Hz) and corresponds to an isolated peak in the power spectrum. This frequency is compatible with the rotation frequency ($f_{\text{rot}} = 0.75 \pm 0.32 \, \text{c d}^{-1}$) determined from spectral fitting. However, this frequency is also detected in spectroscopy in the line-profile variations as well as in spectral quantities, and the amplitude and phase distributions observed in the line-profile variations with this frequency (Fig. 10) are typical of non-radial pulsations with a mode degree $\ell \sim 3$. The CoRoT light curve folded in phase with this frequency is sinusoidal (Fig. 8) and no harmonic of this frequency is detected even though it corresponds to a high amplitude peak, which is also an indication of pulsation rather than rotation. A phase shift of 0.28 in a period is observed between the variation with this frequency in the radial velocity measured in spectral lines and the one observed in the CoRoT light curve (Fig. 12). In terms of non-radial pulsations this phase shift can be explained by non-adiabatic effects (see Dupret et al. 2003), time-variable frequencies, or resonant phase-locking. We thus conclude that the frequency $f_1 = 0.695 \, \text{c d}^{-1}$ is due to non-radial pulsations with a typical $\ell \sim 3$. We note that, in rapidly rotating stars, g-modes with $\ell$ values of 3 or more can be detected, even if lower degree modes (e.g. $\ell = 0$) are not detected, because of the coupling between modes (see Daszyńska-Daszkiewicz et al. 2002).

The frequency peak with the highest amplitude (1.3 mmag) is detected at $f_2 = 0.624 \, \text{c d}^{-1}$ (7.22 $\mu$Hz). Several other frequency peaks are situated just below this frequency, so that it constitutes an entire group of close frequencies. This group includes in particular a frequency at $f_3 = 0.575 \, \text{c d}^{-1}$ (6.65 $\mu$Hz). For rapid rotators such as HD 181231, groups of close frequencies are expected from modes of non-radial pulsations with different $\ell$ values but the same azimuthal order $m$, since the rotational splitting is of the order of $f_{\text{rot}}$. The second, third, and fourth harmonics of $f_2$ are also detected. We note that $2f_2$ has an even stronger amplitude than $f_2$ itself. The CoRoT light curve folded in phase with this frequency is a double sinuoidal wave (Fig. 8). Harmonics can appear in photometry either if the main frequency corresponds to the rotation frequency or if it corresponds to a pulsation frequency with $\ell = 0$ or of a high amplitude. In this case, $f_2$ is compatible with the rotation frequency ($f_{\text{rot}} = 0.75 \pm 0.32 \, \text{c d}^{-1}$) determined from spectral fitting, but since the amplitude of this frequency peak is high it could also be attributed to pulsations. Since $f_2$ has not been detected by our
analysis of the available spectroscopy, we cannot draw firm conclusions on this matter. Seismic modelling is therefore required.

We note that the results for \( f_1 \) and \( f_2 \) show the importance of acquiring spectroscopic observations simultaneously with space photometric observations.

Many combinations of frequencies are also detected as significant peaks in the Fourier analysis of the CoRoT light curve, in particular those resulting from the difference between \( f_2 \) and \( f_1 \) or the other peaks in the group around \( f_1 \). Frequencies detected close to high amplitude peaks could also be caused by changes in the amplitude or phase of the main frequencies.

5.2. Beating effects

Two longer-term variations are observed in the CoRoT data at \( \sim 14 \) days and \( \sim 116 \) days (see Fig. 1). The \( \sim 14\mathrm{d} \) period is clearly visible in the CoRoT light curve (Fig. 1). A frequency for this signal of \( f = 0.07 \cdd\), i.e., 0.8 \( \mu \)Hz, is detected in the analysis of the CoRoT light curve and corresponds to the difference between the two main frequency peaks at \( f_1 = 0.695 \) and \( f_2 = 0.624 \cdd\. Therefore, this can be clearly identified as a beating phenomenon between the two main frequency of variations.

This frequency is also detected in our spectroscopic analysis in the variation of the intensity of \( \alpha \) emission (Fig. 6). This quantity provides direct insight into the circumstellar environment. Therefore, it seems that the beating effect influences the circumstellar environment. A correlation between pulsation properties and Be outbursts was observed in the star HD 49330 (Huat et al. 2009). We note also that the beating frequency corresponds to a tenth of \( f_1 \), which is probably a coincidence.

The \( \sim 116\mathrm{d} \)-period is visible in the CoRoT light curve (Fig. 1) as well as in the 3D representation shown in Fig. 9. The frequency of this signal (\( f \approx 0.00848 \cdd\), i.e., 0.098 \( \mu \)Hz) is detected in the analysis of the CoRoT light curve and corresponds to the difference between \( f_2 = 0.624 \cdd \) and lower amplitude peaks around \( f_1 \) namely \( f_5 \) and \( f_9 \). Frequencies of different \( \ell \) degree values but identical azimuthal order \( m \) are expected to be close frequencies for fast rotators. Moreover, a coupling between frequencies as close as those and with a \( \ell \) difference of 2 is expected (Daszyńska-Daszkiewicz et al. 2002; Soufi et al. 1998). Alternatively, according to seismic modelling performed by Saio and collaborators (e.g. Cameron et al. 2008), one could consider \( f \approx 0.00848 \cdd \) to be a pulsation mode with \( m = 0 \). Hence, \( f_5 \) and \( f_9 \) would then be the combination frequencies of this zonal mode and \( f_2 \).

6. Conclusions

Thanks to the long duration and high photometric accuracy of the CoRoT observations of the Be star HD 181231, we have detected a large number of variation frequencies. This list of 54 detected frequencies can be reduced to a set of at least 10 independent frequencies corresponding to the intrinsic variation frequencies of the star. For each frequency, we have determined the average amplitude and phase during the observing run. One of these frequencies (\( f_1 \)) is also detected by our analysis of the available spectroscopic data, which allows us to identify it as a pulsation mode with a typical \( \ell \) value of ~3. Other lower amplitude peaks are probably also caused by non-radial pulsation modes. A high amplitude frequency peak (\( f_2 \)) could be attributed to either rotation or pulsations.

In addition, we have shown that a beating effect occurs between the two strongest frequencies (\( f_1 \) and \( f_2 \)) with a period of about 14 days. A longer-term beating (116 days) is also observed.

By analysing the spectroscopic data acquired for this work, we have also determined more precisely the fundamental parameters of the star. These results and the seismic results presented above will allow us to calculate models of the interior of this star. This will be the subject of a forthcoming paper.

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