Search for $B \to K^{(*)}\nu\bar{\nu}$ and invisible quarkonium decays

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We search for the flavor-changing neutral-current decays $B \to K^{(*)} \nu \bar{\nu}$, and the invisible decays $J/\psi \to \nu \bar{\nu}$ and $\psi(2S) \to \nu \bar{\nu}$ via $B \to K^{(*)} J/\psi$ and $B \to K^{(*)} \psi(2S)$ respectively, using a data sample of $471 \times 10^6$ $B \bar{B}$ pairs collected by the BABAR experiment. We fully reconstruct the hadronic decay of one of the $B$ mesons in the $T(4S) \to B \bar{B}$ decay, and search for the $B \to K^{(*)} \nu \bar{\nu}$ decay in the rest of the event. We observe no significant excess of signal decays over background and report branching fraction upper limits of $3.7 \times 10^{-5}$, $8.1 \times 10^{-5}$, $9.3 \times 10^{-5}$, and combined upper limits of $3.2 \times 10^{-5}$ all at the 90% confidence level. For the invisible quarkonium decays, we report branching fraction upper limits of $3.9 \times 10^{-3}$ and $15.5 \times 10^{-3}$ at the 90% confidence level. Using the improved kinematic resolution achieved from hadronic reconstruction, we also provide partial branching fraction limits for the $B \to K^{(*)} \nu \bar{\nu}$ decays over the full kinematic spectrum.

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I. INTRODUCTION

Flavor-changing neutral-current transitions, such as $b \to s \ell \nu$, are prohibited in the standard model (SM) at tree-level. However, they can occur via one-loop box or electroweak penguin diagrams, as shown in Fig. 1. They can occur also in the SM via a quarkonium resonance state $b \to s \ell \nu$, where the $\ell \nu$ decay is mediated by a virtual $Z^0$ boson (Fig. 2). This latter decay process has the same final state as $b \to s \nu \bar{\nu}$ with an additional constraint from the on-shell $c \bar{c}$ mass. Both the $b \to s \nu \bar{\nu}$ and $c \bar{c} \to \nu \bar{\nu}$ decay rates are expected to be small within the SM, with branching fractions estimated to be $B(B^+ \to K^+ \nu \bar{\nu}) = B(B^0 \to K^0 \nu \bar{\nu}) = (4.5 \pm 0.7) \times 10^{-6}$, $B(B^+ \to K^{*+} \nu \bar{\nu}) = B(B^0 \to K^{*0} \nu \bar{\nu}) = (6.8^{+1.1}_{-0.9}) \times 10^{-6}$, and $B(J/\psi \to \nu \bar{\nu}) = (4.54 \times 10^{-7}) \cdot B(J/\psi \to e^+ e^-)$.

The $b \to s \nu \bar{\nu}$ rates are predicted with smaller theoretical uncertainties than those in the corresponding $b \to s \ell^+ \ell^-$ modes due to the absence of long-distance hadronic effects from electromagnetic penguin contributions.

Various new-physics scenarios exist that could significantly enhance the $b \to s \nu \bar{\nu}$ branching fractions, as well as modify the expected SM decay distributions of $s_B \equiv q^2/m_B^2$, where $q^2$ is the squared magnitude of the four-momentum transferred from the $B$ meson to

![FIG. 1: Lowest-order SM Feynman diagrams for $b \to s \nu \bar{\nu}$ transitions. The virtual top quark provides the dominant contribution in each case.](image-url)
the neutrino pair, and $m_B$ is the $B$ meson mass. Some of these scenarios predict massive particles that could contribute additional loop diagrams with similar amplitudes as those in the SM, such as nonstandard $Z^0$ couplings with supersymmetric (SUSY) particles $^1$, fourth-generation quarks $^3$, anomalous top-charm transitions $^4$, or a massive $U(1)$ gauge boson $Z'$ $^1$. Since $b \to s\nu\tau$ has two final-state neutrinos, other sources of new physics can also contribute to the experimental signature of a kaon and missing four-momentum, such as low-mass dark-matter (LDM) candidates $^1,6–8$, unparticles $^9$, right-handed neutrinos $^9$, or SUSY particles $^10$. Models with a single universal extra dimension also predict higher decay rates $^1$.

The decays $J/\psi \to \nu\tau$ and $\psi(2S) \to \nu\tau$ provide additional windows for new-physics searches. In spontaneously-broken SUSY, a $c\bar{c}$ resonance can decay into a pair of goldstinos via either a virtual $Z^0$ in the $s$-channel or a $c$-squark exchange in the $t$-channel $^2$ (Fig. 2). The contribution of a massive SU(2) gauge boson $Z'$, introduced in the left-right SUSY model, could suppress the decay rates up to an order of magnitude $^2$. Conversely, a low-mass $U(1)$ gauge boson $U$ could enhance the invisible decay rates of quarkonium states by several orders of magnitude by coupling to LDM particles $^12,13$. The $U$ boson could decay into a pair of spin-$1/2$ Majorana ($\chi\chi$), spin-$1/2$ Dirac ($\chi\bar{\tau}$), or spin-0 ($\varphi\varphi$) LDM particles.

We search for $B \to K\nu\tau$ and $B \to K^+\nu\bar{\tau}$, and for $J/\psi \to \nu\tau$ and $\psi(2S) \to \nu\tau$ via $B \to K^{(*)}\psi(2S)$ respectively, where $K^{(*)}$ signifies a charged or neutral $K$ or $K^*$ meson $^14$. We use a technique in which one $B$ meson is exclusively reconstructed in a hadronic final state before looking for a signal decay within the rest of the event. Since the four-momentum of one $B$ meson is fully determined, the missing mass resolution on the two final-state neutrinos and the suppression of background are improved with respect to other reconstruction techniques.

Several previous searches for $B \to K\nu\tau$ and $B \to K^+\nu\bar{\tau}$ have been performed by both the B$\bar{A}$B$\bar{A}$ and BELLE collaborations $^15,16$. Currently, the most stringent published upper limits at 90% confidence level (CL) are $\mathcal{B}(B^+ \to K^+\nu\bar{\tau}) < 1.3 \times 10^{-5}$ $^13$ and $\mathcal{B}(B \to K^+\nu\bar{\tau}) < 8 \times 10^{-5}$ $^14$. The $\mathcal{B}(B^+ \to K^+\nu\bar{\tau})$ limit was determined using semileptonic-tag reconstruction, which produces samples that are statistically larger and independent of those produced using the hadronic-tag reconstruction employed in this search. The $\mathcal{B}(B \to K^+\nu\bar{\tau})$ limit was a combination of two B$\bar{A}$B$\bar{A}$ analyses, one using semileptonic-tag reconstruction and the other using hadronic-tag reconstruction.

A $J/\psi \to \nu\tau$ search via $\psi(2S) \to \pi^+ \pi^- J/\psi$ was performed by the BES collaboration, which set an upper limit at 90% CL of $\mathcal{B}(J/\psi \to \nu\tau) < 1.2 \times 10^{-3} \cdot \mathcal{B}(J/\psi \to \mu^+\mu^-)$ $^20$. This article presents the first search for $J/\psi \to \nu\tau$ using the hadronic-tag reconstruction of a $B$ meson decay. A search for $\psi(2S) \to \nu\tau$ has not been performed previously.

II. THE B$\bar{A}$B$\bar{A}$ DETECTOR AND DATA SAMPLE

This search uses a data sample of 471 ± 3 million $B\bar{B}$ pairs, corresponding to an integrated luminosity of 429 fb$^{-1}$ collected at the $\Upsilon(4S)$ resonance $^21$. The data were recorded with the B$\bar{A}$B$\bar{A}$ detector $^22$ at the PEP-II asymmetric-energy $e^+e^-$ storage rings. The charged-particle tracking system consists of a five-layer double-sided silicon vertex tracker and a 40-layer drift chamber, both coaxial with a 1.5 T solenoidal magnetic field. Charged kaons and pions are distinguished by specific ionization energy-loss measurements from the tracking system for lower momentum particles, and by measurements from a ring-imaging Cherenkov radiation detector for higher momentum particles. A CsI(Tl) electromagnetic calorimeter is used to reconstruct photons of energy greater than 20 MeV and to identify electrons. Muon identification is provided by the instrumented flux return of the magnet. Particle identification (PID) algorithms are trained to identify charged particle types by using 36 input parameters including momentum, polar and azimuthal angles, the Cherenkov angle, and energy-loss measurements $^23$. We employ PID criteria that select $K^+$ mesons with an efficiency greater than 85% and with approximately 1% misidentification probability for pions and muons.

Signal and background decays are studied using Monte Carlo (MC) samples simulated with Geant4 $^24$. The simulation includes a detailed model of the B$\bar{A}$B$\bar{A}$ detector geometry and response. Beam-related background and detector noise are extracted from data and are overlaid on the MC simulated events. Large MC samples of generic $B\bar{B}$ and continuum $(e^+e^- \to \tau^+\tau^-)$ or $e^+e^- \to q\bar{q}$ events provide ten times the number of $\Upsilon(4S) \to B\bar{B}$ and $e^+e^- \to c\bar{c}$ events as in the data sample, and four times the number of other continuum decays. The $\Upsilon(4S) \to B\bar{B}$ signal MC samples are generated with one $B$ meson decaying via $B \to K^{(*)}\nu\tau$, with and without the $c\bar{c}$ resonances, while the other $B$ meson decays according to a model tuned to world averages of allowed decay channels. The $s_B$ distributions

![FIG. 2: Lowest-order Feynman diagrams of (from left to right) the SM decay $c\bar{c} \to \nu\tau$, the SUSY decay $c\bar{c}$ into a pair of goldstinos ($\tilde{g}$) via a $c$-squark in the $t$-channel, and the SUSY decay $c\bar{c} \to \tilde{g}\tilde{g}$ via a virtual $Z^0$ in the $s$-channel.](image)
for $B \rightarrow K^{(*)}\nu\overline{\nu}$ decays with signal MC samples are generated initially using a phase-space model, and then reweighted using the model from Ref. [1], henceforth referred to as ABSW. Within $B \rightarrow K^{(*)}\nu\overline{\nu}$ decays, this model is also used to reweight the helicity-angle distribution between the signal $B$ and the $K^+$ or $K^0$ flight directions in the $K^*$ rest frame. The helicity amplitudes for the decay channels $B \rightarrow K^*J/\psi$ and $B \rightarrow K^*\psi(2S)$ are generated using values taken from a BABAR measurement [22].

III. ANALYSIS METHOD

Event selection for both the $B \rightarrow K^{(*)}\nu\overline{\nu}$ and $B \rightarrow K^{(*)}\rho$ searches begins by fully reconstructing a $B$ meson ($B_{\text{tag}}$) in one of many hadronic final states, $B \rightarrow SX_{\text{had}}^+$, where $S$ is a “seed” meson ($D^{(*)+}$, $D^{(*)0}$, $D_s^{(*)+}$, or $J/\psi$) and $X_{\text{had}}^+$ is a collection of at most five mesons, composed of charged and neutral kaons and pions with a net charge of $-1$. This method, which was used also in Ref. [20], reconstructs additional modes with respect to previous hadronic-tag $B \rightarrow K^{(*)}\nu\overline{\nu}$ analyses [16, 17], and results in approximately twice the reconstruction efficiency. The $D$ seeds are reconstructed in the decay modes $D^+ \rightarrow K^0\pi^+$, $K^0\pi^+\pi^0$, $K^0\pi^+\pi^+\pi^-$, $K^-\pi^+\pi^+\pi^-$, $K^-\pi^+\pi^+\pi^+$, $K^+K^-\pi^+$, $K^+K^-\pi^+\pi^0$; $D^0 \rightarrow K^-\pi^+$, $K^-\pi^+\pi^0$, $K^-\pi^+\pi^+\pi^-$, $K^0\pi^+\pi^-$, $K^0\pi^+\pi^-\pi^0$, and $K^0\pi^-\pi^-\pi^0$. Additional seeds are reconstructed as $D^{*+} \rightarrow D^0\pi^+$, $D^+\pi^0$, $D^{*0} \rightarrow D^0\pi^0$, $D^{*0}\gamma$; $D_s^{*+} \rightarrow D_s^+\pi^0$; $D_s^+ \rightarrow \phi[\rightarrow K^+K^-]\pi^+$, $K^0K^+$; and $J/\psi \rightarrow e^+e^-$, $\mu^+\mu^-$. The $K^0_{\text{S}}$ candidates are reconstructed via their decay to $\pi^+\pi^-$. 

Well-reconstructed $B_{\text{tag}}$ candidates are selected using two kinematic variables: $\Delta E = E_{B_{\text{tag}}} - \sqrt{s}/2$ and $m_{\text{ES}} = \sqrt{s}/4 - \vec{p}_{B_{\text{tag}}}^2$, where $E_{B_{\text{tag}}}$ and $\vec{p}_{B_{\text{tag}}}$ are the energy and momentum vector of the $B_{\text{tag}}$ candidate, respectively, in the $e^+e^-$ center-of-mass (CM) frame and $\sqrt{s}$ is the total energy of the $e^+e^-$ system. The value of $\Delta E$, which peaks at zero for correctly reconstructed $B$ mesons, is required to be between $-0.12$ and $0.12$ GeV or within two standard deviations around the mean for a given $X_{\text{had}}^-$ mode, whichever is the tighter constraint. If more than one $B_{\text{tag}}$ candidate is reconstructed, the one in the mode with the highest purity (fraction of candidates that are correctly reconstructed within a given $B_{\text{tag}}$ decay mode) is chosen. If there are multiple candidates with the same purity, the one with the smallest $|\Delta E|$ is selected.

After requiring that the event contains between one and three charged tracks not used in the $B_{\text{tag}}$ reconstruction (“signal-side” tracks), the purity of each mode is recalculated, and only the $B_{\text{tag}}$ modes that have a re-calculated purity greater than 68% are retained. This results in a total of 448 final states. This purity value was optimized by maximizing the figure of merit [27]

$$\epsilon_i^{\text{sig}} = \frac{1}{\sigma_n + \sqrt{N_i^{\text{bkg}}}}$$

where the number of sigmas $n_{\sigma} = 1.28$ corresponds to a one-sided Gaussian limit at 90% CL, $\epsilon_i^{\text{sig}}$ is the total signal efficiency, and $N_i^{\text{bkg}}$ is the expected number of background events, with $i$ representing one of the signal decay channels. All other selection criteria discussed henceforth were optimized simultaneously using this same figure of merit.

The signal region of the $B_{\text{tag}}$ candidate is defined as $5.273 < m_{\text{ES}} < 5.290$ GeV/c$^2$ (Fig. 3), since correctly reconstructed $B$ mesons produce a peak in this region near the nominal $B$-meson mass. The $B_{\text{tag}}$ candidates that are incorrectly reconstructed (“combinatorial” events), which result from continuum events or are due to particles assigned to the wrong $B$ meson, produce a distribution that is relatively uniform below the $m_{\text{ES}}$ signal region and decreases toward the kinematic limit within it. Approximately 0.3% of signal MC events and 12.0 million data events contain a $B_{\text{tag}}$ that is reconstructed using the above requirements and found to be within the $m_{\text{ES}}$ signal region. Since $B$ mesons are spin zero and are produced with low momentum in the CM frame ($\sim 0.32$ GeV/c), their decay products are more isotropically distributed than non-$B\overline{B}$ background. For example, $|\cos \theta_T|$, where $\theta_T$ is the angle in the CM frame between the $B_{\text{tag}}$ thrust axis and the thrust axis of all other particles in the event, has a uniform distribution for $B\overline{B}$ events but peaks near one for continuum events. Continuum background is sup-
pressed by using a multivariate likelihood selector based on six event-shape variables. These consist of $|\cos(\theta_f)|$, the cosine of the angle between $\vec{p}_{\text{miss}}$ and the beam axis, the magnitude of the $B_{\text{tag}}$ thrust, the component of the $B_{\text{tag}}$ thrust along the beam axis, the angle between the missing momentum vector ($\vec{p}_{\text{miss}}$) and the beam axis, and the ratio of the second-to-zeroth Fox-Wolfram moment computed using all charged and neutral particles in the event. The multivariate selector requires

$$L_B \equiv \frac{\prod_j P_B(x_j)}{\sum_j P_B(x_j) + \prod_j P_q(x_j)} > 53\%,$$

where $P_q(x_j)$ and $P_B(x_j)$ are probability density functions determined from MC that describe continuum and signal-like $B\overline{B}$ events, respectively, for the six event-shape variables $x_j$. The $L_B$ requirement, which was optimized with other selection criteria using Eq. (1), also improves the agreement between data and MC by suppressing unmodeled continuum backgrounds.

In the sample of selected $B_{\text{tag}}$ candidates, signal events are chosen such that a single $K^{(*)}$ candidate can be reconstructed within the rest of the event and no additional charged tracks remain in the event. The sum of the $K^{(*)}$ and $B_{\text{tag}}$ candidate charges must equal zero. Since signal decays have two final-state neutrinos, these events are required to have missing energy greater than zero, where the missing energy is defined as the CM energy minus all detected calorimeter deposits from charged and neutral particles in the event. For $B \to K^{(*)}\overline{\nu}\nu$, the signal decays are reconstructed in six channels: $B^+ \to K^+\nu\overline{\nu}$, $B^0 \to K^0\nu\overline{\nu}$ where $K^0 \to K^0\pi^0$, $B^+ \to K^+\pi^0\nu\overline{\nu}$, where $K^{*+} \to K^{*+}\pi^0$ and $K^{*+} \to K^{*0}\pi^+$; and $B^0 \to K^{0}\nu\overline{\nu}$, where $K^{0} \to K^+\pi^-$ and $K^{0} \to K^0\pi^0$. For $c\pi \to \nu\pi$, the same six signal channels are employed with an additional requirement that the $K^{(*)}$ momentum is consistent with a two-body decay, either $B \to K^{(*)}\psi(2S)$ or $B \to K^{(*)}\psi(2S)$. The $\psi$ and $\psi(2S)$ mesons then decay into a pair of neutrinos, thus yielding the same final states as for $B \to K^{(*)}\overline{\nu}\nu$.

We reconstruct $K^{0}\rightarrow \pi^{+}\pi^{-}\pi^{0}$ decay candidates using two tracks of opposite charge, which originate from a common vertex and produce an invariant mass within $\pm7$ MeV/$c^2$ of the nominal $K^{0}$ mass. The PID for each track must be inconsistent with that for an electron, muon, or kaon. The $\pi^{0}$ candidates are reconstructed from pairs of photon candidates with individual energies greater than 30 MeV, a total CM energy greater than 200 MeV, and a $\gamma\gamma$ invariant mass between 100 and 160 MeV/$c^2$. All $K^{+}$ candidates must satisfy the PID criteria for a kaon.

Reconstructed $K^{*}$ candidates are required to have an invariant mass within $\pm70$ MeV/$c^2$ of the nominal $K^{*}$ mass. A $K^{*+} \rightarrow K^{0}\pi^{+}$ candidate combines a $K^{0}$ candidate with a track that satisfies the PID criteria for a pion. If more than one $K^{*+} \rightarrow K^{0}\pi^{+}$ candidate can be reconstructed in an event, the one with the mass closest to the nominal $K^{*+}$ mass is chosen. A $K^{*0} \rightarrow K^{+}\pi^{-}$ candidate combines one track that satisfies the PID criteria for a kaon with one that is inconsistent with the PID criteria for an electron, muon, or kaon. In an event containing a $K^{+} (K^{0})$ candidate and no additional signal-side tracks, $K^{*} \rightarrow K^{*+}\pi^{0} (K^{*0}\pi^{0})$ candidates are reconstructed if the invariant mass of a $\pi^{0}$ candidate and the $K^{+} (K^{0})$ candidate falls within the $K^{*}$ mass window; otherwise the event is considered for the $K^{+} (K^{0})$ signal channel. If more than one $K^{+} \rightarrow K^{*+}\pi^{0}$ or $K^{0} \rightarrow K^{*0}\pi^{0}$ candidate can be reconstructed, the one with the highest energy $\pi^{0}$ candidate is chosen.

Once the $B_{\text{tag}}$ and $K^{(*)}$ are identified, the signal events are expected to contain little or no additional energy within the calorimeter. However, additional energy deposits can result from beam-related photons, hadronic shower fragments that were not reconstructed into the primary particle deposit, and photons from unreconstructed $D^{*} \rightarrow D\gamma/\pi^{0}$ transitions in the $B_{\text{tag}}$ candidate. Only deposits with energy greater than 50 MeV in the rest frame of the detector are considered, and the sum of all such additional energy deposits ($E_{\text{extra}}$) is required to be less than a threshold value ($E_{t}$). The values of $E_{t}$, given in Table I and depicted in Fig. I were optimized with the other selection criteria but were allowed to differ between signal channels. For events within the $K^{*}$ signal channel, calorimeter deposits identified as kaon shower fragments are not included in the $E_{\text{extra}}$ sum. A fragment candidate is defined as a neutral calorimeter deposit whose momentum vector, when compared to that of the signal track, is separated by polar and azimuthal angles (relative to the beam axis and in the rest frame of the detector) of $\Delta\theta$ and $\Delta\phi$, respectively, such that $r_{\text{clus}} < 15^\circ$, where $r_{\text{clus}} \equiv \sqrt{(\Delta\theta)^2 + \frac{2}{3}(Q_{K} \cdot \Delta\phi - 8\pi)^2}$ and $Q_{K} = \pm1$ is the $K^{*}$ charge. The $r_{\text{clus}}$ and fragment candidate definitions were optimized using studies of truth information in the signal MC samples. The recovery of these kaon shower fragments improves the final signal efficiency in the $K^{*}$ channel by about 13%. This procedure was explored for the other signal tracks, but the effect was small.

<table>
<thead>
<tr>
<th>Channel</th>
<th>$K^{+}$</th>
<th>$K^{0}$</th>
<th>$K^{*+}\pi^{0}$</th>
<th>$K^{*0}\pi^{0}$</th>
<th>$K^{+}\pi^{-}$</th>
<th>$K^{0}\pi^{0}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$E_{t}$ [GeV]</td>
<td>0.11</td>
<td>0.28</td>
<td>0.18</td>
<td>0.29</td>
<td>0.31</td>
<td>0.33</td>
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The searches for $B \rightarrow K^{(*)}\overline{\nu}\nu$ and for $c\pi \rightarrow \nu\pi$ via $B \rightarrow K^{(*)}\overline{\nu}\nu$ diverge in the final step of the signal selection, which involves restricting the kinematics of the decay. The value of $s_{B}$ is calculated as $(p_{B_{\text{tag}}} - p_{K^{(*)}})^2/m_{B}^{2}$, where $p_{K^{(*)}}$ is the four-momentum of the $K^{(*)}$ candidate, and $p_{B_{\text{tag}}}$ is the expected signal $B$ four-momentum with an energy of $\sqrt{s}/2$, the nominal $B$-meson mass, and a momentum vector pointing opposite the $B_{\text{tag}}$ momentum. For $B \rightarrow K^{(*)}\overline{\nu}\nu$, the signal region optimized for
maximum SM sensitivity is $0 < s_B < 0.3$ for all six signal channels. This corresponds to a $K^{(*)}$ momentum greater than about 1.8 (1.7) GeV/c in the signal $B$ rest frame for $B \rightarrow K(\ell)\ell\nu$ ($B \rightarrow K^{(*)}\ell\nu$) events. Partial branching fractions over the full $s_B$ spectrum are also provided for sensitivity to new-physics scenarios that modify the 

FIG. 4: (color online) The $E_{\text{extra}}$ distribution over the full $s_B$ spectrum in the (from top to bottom) $K^+$, $K^0$, $K^{*+}$, and $K^{*0}$ channels after applying all other signal selection criteria. The expected combinatorial (shaded) plus $m_{\text{ES}}$-peaking (solid) background contributions are overlaid on the data (points). The $B \rightarrow K^{(*)}\ell\nu$ signal MC distributions (dashed) have arbitrary normalization. Both the $B \rightarrow K^{(*)}\ell\nu$ and $c\bar{c} \rightarrow \nu\bar{\nu}$ searches select events to the left of the vertical line that corresponds to the $E_1$ value of that channel, as given in Table I.

IV. BACKGROUND AND BRANCHING FRACTION EXTRACTION

The total number of background events $N_i^{\text{bkg}}$ in the signal region has two components: $N_i^{\text{peak}}$ is the number of expected background events having a correctly reconstructed $B_{\text{tag}}$ candidate and hence peaking within the $m_{\text{ES}}$ signal region, and $N_i^{\text{comb}}$ is the number of expected combinatorial background events, including both continuum events and $B\bar{B}$ events with an incorrectly reconstructed $B_{\text{tag}}$ candidate. To reduce the dependence on MC simulations, the number of $N_i^{\text{comb}}$ events is extrapolated directly from the observed data events within the $m_{\text{ES}}$ signal region, defined as $5.200 < m_{\text{ES}} < 5.265$ GeV/c$^2$ and depicted in Fig. B. The shape of the combinatorial $m_{\text{ES}}$ distribution is estimated using MC samples of continuum events and of $B\bar{B}$ events reconstructed with the wrong charge.

The number of $N_i^{\text{peak}}$ events is estimated from generic $B\bar{B}$ MC samples. Over half of $N_i^{\text{peak}}$ is found to be from $B \rightarrow D(\ast)\ell\nu$ ($\ell = e$ or $\mu$) decays in which no lepton candidate is identified in the event and the $K^{(*)}$ is a daughter of the $D$ or $D^*$ meson. One particular peaking background in the $B \rightarrow K(\ast)\ell\nu$ search is $B^+ \rightarrow \tau^+\nu_\tau$, with $\tau^+ \rightarrow K^{(*)}\nu_\tau$, which has the same final state as the signal decay [31]. Exclusive $B^+ \rightarrow \tau^+\nu_\tau$ MC samples, assuming a branching fraction of $(1.65 \pm 0.34) \times 10^{-4}$ [30], indicate that this background constitutes less than 15 ($5\%$) of the total background in the $B^+ \rightarrow K^{(*)}\nu$ ($B^+ \rightarrow K^{*+}\nu$ or $B^+ \rightarrow K^{*+}\nu\bar{\nu}$) channel.

Since both $N_i^{\text{peak}}$ and $\epsilon_i^{\text{sig}}$ are determined from MC samples, we normalize the MC yields to the data to account for differences between data and MC, such as from the $B_{\text{tag}}$ reconstruction and the modeled branching fractions of $B_{\text{tag}}$ modes within the MC. This normalization is performed before applying the full signal selection in order to have a large background-to-signal ratio; looser $K^{(*)}$ mass windows and $E_{\text{extra}}$ selection requirements are used such that the number of background events is approximately 60 times larger than the final background contribution, over the full $s_B$ spectrum. The peaking background component in the $B\bar{B}$ MC is then normalized to the number of data events that peak within the $m_{\text{ES}}$ signal region. This peaking yield normalization is performed separately for charged and neutral $B_{\text{tag}}$ candidates, and results in the scaling of all signal and background MC samples by $1.027 \pm 0.039$ ($1.017 \pm 0.044$) for charged (neutral) $B_{\text{tag}}$ candidates.

The signal branching fractions are calculated using

$$B_i = \frac{N_i^{\text{obs}} - (N_i^{\text{peak}} + N_i^{\text{comb}})}{\epsilon_i^{\text{sig}} N_{B\bar{B}}},$$

where $N_{B\bar{B}} = 471 \times 10^6$ is the total number of $B$ meson pairs in the data sample and $N_i^{\text{obs}}$ is the number of data events within the signal region. The total signal efficiency $\epsilon_i^{\text{sig}}$ includes that of the $B_{\text{tag}}$ reconstruction and
is determined separately for each of the signal channels. Since misreconstructed events from other signal channels contribute to $N_{i}^{\text{peak}}$, the branching fractions of all signal channels are determined simultaneously by inverting a $6 \times 6$ efficiency matrix $\varepsilon_{ij}$, which describes the probability that a signal event of process $i$ is reconstructed in signal channel $j$. Branching fraction limits and uncertainties are computed using a mixed frequentist-Bayesian approach described in Ref. [32], with the systematic uncertainties on $N_{i}^{\text{bkg}}$ and $\varepsilon_{i}^{\text{sig}}$ modeled using Gaussian distributions. To combine the results of signal decay channels, we find the $B_{i}$ value that maximizes a likelihood function defined as the product of the Poisson probabilities of observing $N_{i}^{\text{obs}}$ events.

V. SYSTEMATIC STUDIES

To verify the modeling of $\varepsilon_{i}^{\text{sig}}$ and $N_{i}^{\text{bkg}}$, a control sample of $B \rightarrow D\ell\nu$ events is selected. In place of a signal $K^{*}$ candidate, the events are required to contain a reconstructed $D^{0} \rightarrow K^{-}\pi^{+}$, $D^{-} \rightarrow K^{+}\pi^{-}\pi^{-}$, or $D^{-} \rightarrow K_{S}^{0}\pi^{-}$ candidate with an invariant mass within $\pm$35 MeV/$c^{2}$ of the nominal $D$-meson mass values [31]. The event must have one additional track that satisfies the PID criteria of either an electron or muon. All other reconstruction and signal selection requirements are retained. The resulting yields in the data agree with MC expectations, assuming the well-measured branching fractions of $B \rightarrow D\ell\nu$ [31], within the 7% (12%) statistical uncertainty of the data in the $0 < s_{B} < 0.3$ ($J/\psi$ or $\psi(2S)$ mass) region.

The control sample is used to determine the systematic uncertainties due to the MC modeling of the $E_{\text{extra}}$ variable within data. Additional uncertainties on $N_{i}^{\text{peak}}$ and $\varepsilon_{i}^{\text{sig}}$ are due to the $K_{S}^{0}$ and $K^{*}$ mass reconstruction windows, the $\pi^{0}$ reconstruction, and the uncertainties in the branching fractions [31] of the dominant backgrounds contributing to $N_{i}^{\text{peak}}$. The uncertainty on $N_{i}^{\text{comb}}$ is dominated by the sideband data statistics. Other systematic uncertainties, such as those from PID, tracking, $B_{\text{tag}}$ reconstruction, $N_{BB}$, and the assumption that charged and neutral $B\bar{B}$ pairs are produced at equal rates, are all accounted for by the normalization of the MC peaking yields. Because the peaking yield in data depends on the extrapolated shape of the combinatorial $B_{\text{tag}}$ background, the normalization scale factors are re-evaluated by varying the method used to extrapolate this shape. The resulting variations on the final $N_{i}^{\text{bkg}}$ and $\varepsilon_{i}^{\text{sig}}$ values are taken as the systematic uncertainties due to the normalization.

Due to the approximately 1.0% resolution on the $s_{B}$ measurement around $s_{B} = 0.3$, an uncertainty is evaluated within the $B \rightarrow K^{(*)}\nu\bar{\nu}$ signal region. Similarly, the resolution on $m_{i\nu}$ contributes to uncertainties within the $J/\psi \rightarrow \nu\bar{\nu}$ and $\psi(2S) \rightarrow \nu\bar{\nu}$ signal regions. Only the systematic uncertainties due to the $N_{i}^{\text{peak}}$ branching fractions and to $s_{B}$ or $m_{i\nu}$ differ between the $B \rightarrow K^{(*)}\nu\bar{\nu}$, $J/\psi \rightarrow \nu\bar{\nu}$, and $\psi(2S) \rightarrow \nu\bar{\nu}$ searches. The systematic uncertainties are summarized in Tables [II] and [III]; the former lists the uncertainties shared by the searches, while the latter lists those that differ.

<table>
<thead>
<tr>
<th>Source</th>
<th>$K^{+} [K^{+}\pi^{0}]$</th>
<th>$[K_{S}^{0}\pi^{+}]$</th>
<th>$K^{0} [K^{0}\pi^{-}]$</th>
<th>$[K_{S}^{0}\pi^{0}]$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N_{i}^{\text{peak}}$ $\ell$'s</td>
<td>2.8</td>
<td>2.8</td>
<td>2.8</td>
<td>2.8</td>
</tr>
<tr>
<td>$s_{B}$ resolution</td>
<td>3.6</td>
<td>3.6</td>
<td>3.6</td>
<td>3.6</td>
</tr>
<tr>
<td>Total $N_{i}^{\text{peak}}$ syst.</td>
<td>6.8</td>
<td>8.9</td>
<td>9.7</td>
<td>10.9</td>
</tr>
<tr>
<td>Total $N_{i}^{\text{comb}}$ syst.</td>
<td>2.3</td>
<td>2.3</td>
<td>2.3</td>
<td>6.0</td>
</tr>
<tr>
<td>Total $\varepsilon_{i}^{\text{sig}}$ syst.</td>
<td>6.7</td>
<td>8.8</td>
<td>11.4</td>
<td>11.7</td>
</tr>
<tr>
<td>$J/\psi \rightarrow \nu\bar{\nu}$</td>
<td>$\psi(2S) \rightarrow \nu\bar{\nu}$</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$N_{i}^{\text{peak}}$ $\ell$'s</td>
<td>3.5</td>
<td>3.5</td>
<td>3.5</td>
<td>3.5</td>
</tr>
<tr>
<td>$m_{i\nu}$ resolution</td>
<td>1.1</td>
<td>2.1</td>
<td>0.4</td>
<td>0.7</td>
</tr>
<tr>
<td>Total $N_{i}^{\text{peak}}$ syst.</td>
<td>6.2</td>
<td>8.6</td>
<td>9.3</td>
<td>10.5</td>
</tr>
<tr>
<td>Total $N_{i}^{\text{comb}}$ syst.</td>
<td>2.3</td>
<td>2.3</td>
<td>2.3</td>
<td>6.0</td>
</tr>
<tr>
<td>Total $\varepsilon_{i}^{\text{sig}}$ syst.</td>
<td>5.8</td>
<td>8.3</td>
<td>8.0</td>
<td>10.8</td>
</tr>
</tbody>
</table>

VI. RESULTS FOR $B \rightarrow K^{(*)}\nu\bar{\nu}$

Figure [3] shows the observed data yields, expected background contributions, and SM signal distributions.
upper limits at the 90% CL of
\[ \mathcal{B}(B^+ \to K^+\nu\overline{\nu}) < 1.6 \times 10^{-5}, \]
\[ \mathcal{B}(B^0 \to K^0\nu\overline{\nu}) < 4.9 \times 10^{-5}, \text{ and} \]
\[ \mathcal{B}(B \to K\nu\overline{\nu}) < 1.7 \times 10^{-5}. \] (4)

The combined central value is \( \mathcal{B}(B \to K\nu\overline{\nu}) = (0.8_{-0.7}^{+0.6}) \times 10^{-5} \), where the uncertainty includes both statistical and systematic uncertainties. These combined results reweight the \( s_B \) distribution to that of the ABSW theoretical model (dashed curve in Fig. 5), which decreases the signal efficiencies published in Ref. [15] by approximately 10%. The \( B \to K^*\nu\overline{\nu} \) central values also can be combined with the semileptonic-tag results from a previous \( \text{BaBar} \) search [16]. In order to obtain approximate frequentist intervals, the likelihood functions in the previous search are extended to include possibly negative signals. We obtain combined \( \text{BaBar} \) upper limits at the 90% CL of
\[ \mathcal{B}(B^+ \to K^{*+}\nu\overline{\nu}) < 6.4 \times 10^{-5}, \]
\[ \mathcal{B}(B^0 \to K^{*0}\nu\overline{\nu}) < 12 \times 10^{-5}, \text{ and} \]
\[ \mathcal{B}(B \to K^*\nu\overline{\nu}) < 7.6 \times 10^{-5}. \] (5)
TABLE IV: Expected $B \to K^* \nu \bar{\nu}$ background yields $N_i^{\text{bkg}} = N_i^{\text{peak}} + N_i^{\text{comb}}$, signal efficiencies $\varepsilon_i^{\text{sig}}$, number of observed data events $N_i^{\text{obs}}$, resulting branching fraction upper limits at 90% CL, and the combined upper limits and central values, all within the $0 < s_B < 0.3$ region. Uncertainties are statistical and systematic, respectively. The channels in brackets refer to the $K^*$ decay products.

<table>
<thead>
<tr>
<th>Channel</th>
<th>$B^+ \to [K^+ \pi^0] \nu \bar{\nu}$</th>
<th>$B^0 \to [K^+ \pi^-] \nu \bar{\nu}$</th>
<th>$B^0 \to [K^0 \pi^-] \nu \bar{\nu}$</th>
<th>$B^0 \to [K^0 \pi^0] \nu \bar{\nu}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N_i^{\text{peak}}$</td>
<td>$1.2 \pm 0.4 \pm 0.1$</td>
<td>$1.3 \pm 0.4 \pm 0.1$</td>
<td>$5.0 \pm 0.8 \pm 0.5$</td>
<td>$0.2 \pm 0.2 \pm 0.0$</td>
</tr>
<tr>
<td>$N_i^{\text{comb}}$</td>
<td>$1.1 \pm 0.4 \pm 0.0$</td>
<td>$0.8 \pm 0.3 \pm 0.0$</td>
<td>$2.0 \pm 0.5 \pm 0.1$</td>
<td>$0.5 \pm 0.3 \pm 0.0$</td>
</tr>
<tr>
<td>$N_i^{\text{bkg}}$</td>
<td>$2.3 \pm 0.5 \pm 0.1$</td>
<td>$2.0 \pm 0.5 \pm 0.1$</td>
<td>$7.0 \pm 0.9 \pm 0.5$</td>
<td>$0.7 \pm 0.3 \pm 0.0$</td>
</tr>
<tr>
<td>$\varepsilon_i^{\text{sig}} \times 10^{-5}$</td>
<td>$4.9 \pm 0.2 \pm 0.4$</td>
<td>$6.0 \pm 0.2 \pm 0.5$</td>
<td>$12.2 \pm 0.3 \pm 1.4$</td>
<td>$1.2 \pm 0.1 \pm 0.1$</td>
</tr>
<tr>
<td>$N_i^{\text{obs}}$</td>
<td>$3$</td>
<td>$3$</td>
<td>$7$</td>
<td>$2$</td>
</tr>
<tr>
<td>Limit</td>
<td>$&lt; 19.4 \times 10^{-5}$</td>
<td>$&lt; 17.0 \times 10^{-5}$</td>
<td>$&lt; 8.9 \times 10^{-5}$</td>
<td>$&lt; 86 \times 10^{-5}$</td>
</tr>
<tr>
<td>$B(B^{+/0} \to K^{+/0} \nu \bar{\nu})$</td>
<td>$(3.3^{+6.2+1.7}_{-3.6-1.3}) \times 10^{-5}$</td>
<td>$(2.9^{+2.2+2.0}_{-1.9-0.9}) \times 10^{-5}$</td>
<td>$(2.7^{+3.8+1.2}_{-2.9-1.0}) \times 10^{-5}$</td>
<td>$&lt; 9.3 \times 10^{-5}$</td>
</tr>
<tr>
<td>Limit</td>
<td>$&lt; 11.6 \times 10^{-5}$</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>$B(B \to K^* \nu \bar{\nu})$</td>
<td></td>
<td></td>
<td></td>
<td>$&lt; 7.9 \times 10^{-5}$</td>
</tr>
</tbody>
</table>

FIG. 6: The central values (points with 1σ error bars) of the partial branching fractions $\Delta B_i$ versus $s_B$, for (a) $B^+ \to K^+ \nu \bar{\nu}$, (b) $B^0 \to K^0 \nu \bar{\nu}$, (c) $B^+ \to K^+ \nu \bar{\nu}$, and (d) $B^0 \to K^0 \nu \bar{\nu}$. The subplots show the distribution of the final signal efficiencies within each $s_B$ interval (histogram with error bars) and over the full $s_B$ spectra (dotted line). The partial branching fractions are provided only within the intervals that are unaffected by the kinematic limit at large $s_B$.

TABLE V: Expected $B \to K \nu \bar{\nu}$ background yields $N_i^{\text{bkg}} = N_i^{\text{peak}} + N_i^{\text{comb}}$, signal efficiencies $\varepsilon_i^{\text{sig}}$, number of observed data events $N_i^{\text{obs}}$, resulting branching fraction upper limits at 90% CL, the central values $B_i$, and the combined upper limits and central value, all within the $0 < s_B < 0.3$ region. Lower limits at 90% CL are also reported, as discussed in the text. Uncertainties are statistical and systematic, respectively. The $B^0 \to K^0 \nu \bar{\nu}$ efficiency accounts for $B(K^0 \to K^0)$ and $B(K^0 \to K^0) (\text{BR})$.

<table>
<thead>
<tr>
<th>Channel</th>
<th>$B^+ \to K^+ \nu \bar{\nu}$</th>
<th>$B^0 \to K^0 \nu \bar{\nu}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N_i^{\text{peak}}$</td>
<td>$1.8 \pm 0.4 \pm 0.1$</td>
<td>$2.0 \pm 0.5 \pm 0.2$</td>
</tr>
<tr>
<td>$N_i^{\text{comb}}$</td>
<td>$1.1 \pm 0.4 \pm 0.0$</td>
<td>$0.9 \pm 0.4 \pm 0.1$</td>
</tr>
<tr>
<td>$N_i^{\text{bkg}}$</td>
<td>$2.9 \pm 0.6 \pm 0.1$</td>
<td>$2.9 \pm 0.6 \pm 0.2$</td>
</tr>
<tr>
<td>$\varepsilon_i^{\text{sig}} \times 10^{-5}$</td>
<td>$43.8 \pm 0.7 \pm 3.0$</td>
<td>$10.3 \pm 0.2 \pm 1.2$</td>
</tr>
<tr>
<td>$N_i^{\text{obs}}$</td>
<td>$6$</td>
<td>$3$</td>
</tr>
<tr>
<td>$B_i$</td>
<td>$(1.5^{+1.7+0.4}_{-1.8-0.2}) \times 10^{-5}$</td>
<td>$(0.14^{+0.0+1.7}_{-0.9-0.9}) \times 10^{-5}$</td>
</tr>
<tr>
<td>Limits</td>
<td>$(&gt; 0.4, &lt; 3.7) \times 10^{-5}$</td>
<td>$&lt; 8.1 \times 10^{-5}$</td>
</tr>
<tr>
<td>$B(B \to K \nu \bar{\nu})$</td>
<td>$(1.4^{+1.4+0.0}_{-0.9-0.2}) \times 10^{-5}$</td>
<td></td>
</tr>
<tr>
<td>Limits</td>
<td>$(&gt; 0.2, &lt; 3.2) \times 10^{-5}$</td>
<td></td>
</tr>
</tbody>
</table>

The $B \to K^\ast \nu \bar{\nu}$ upper limits from this search improve the constraints from previous searches on the Wilson-coefficient parameter space, as shown in Fig. 7. The $B \to K \nu \bar{\nu}$ lower limit provides the first upper bound on $\eta$ and lower bound on $\epsilon$. These constraints are consistent with the expected SM values of $\epsilon = 1$ and $\eta = 0$.

VII. RESULTS FOR $C^\ast \to \nu \bar{\nu}$

In the search for $C^\ast \to \nu \bar{\nu}$, Fig. 8 shows the $m_{\nu \bar{\nu}}$ distribution of the observed data yields, expected background contributions, and SM signal distributions. Tables VI and VII summarize the background contribution values and signal efficiencies within the $J/\psi$ and $\psi(2S)$...
TABLE VI: Expected $J/\psi \to \nu \pi$ background yields $N_i^{\text{peak}}$ and $N_i^{\text{bkg}}$, signal efficiencies $\varepsilon_i^{\text{sig}}$, number of observed data events $N_i^{\text{obs}}$, and the resulting branching fraction central value and upper limit at 90% CL, all within the $m_{\pi\pi}$ invariant mass region corresponding to the $J/\psi$ mass. Uncertainties are statistical and systematic, respectively. The $N_i^{\text{comb}}$ yields are calculable as $N_i^{\text{bkg}} - N_i^{\text{peak}}$.

<table>
<thead>
<tr>
<th>Channel</th>
<th>$K^+$</th>
<th>$K^0$</th>
<th>$K^{*+} \to K^+\pi^0$</th>
<th>$K^{*+} \to K^0\pi^+$</th>
<th>$K^{*0} \to K^+\pi^-$</th>
<th>$K^{*0} \to K^0\pi^0$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N_i^{\text{peak}}$</td>
<td>0.4 ± 0.2 ± 0.0</td>
<td>0.7 ± 0.3 ± 0.1</td>
<td>0.8 ± 0.3 ± 0.1</td>
<td>0.4 ± 0.2 ± 0.0</td>
<td>2.6 ± 0.5 ± 0.3</td>
<td>0.6 ± 0.2 ± 0.1</td>
</tr>
<tr>
<td>$N_i^{\text{bkg}}$</td>
<td>0.5 ± 0.2 ± 0.0</td>
<td>0.7 ± 0.3 ± 0.1</td>
<td>0.8 ± 0.3 ± 0.1</td>
<td>0.8 ± 0.3 ± 0.0</td>
<td>2.8 ± 0.5 ± 0.3</td>
<td>0.6 ± 0.2 ± 0.1</td>
</tr>
<tr>
<td>$\varepsilon_i^{\text{sig}} (\times 10^{-8})$</td>
<td>95.3 ± 4.4 ± 5.5</td>
<td>19.3 ± 1.0 ± 2.1</td>
<td>20.9 ± 1.5 ± 1.7</td>
<td>12.4 ± 0.8 ± 1.0</td>
<td>36.2 ± 1.9 ± 4.0</td>
<td>1.8 ± 0.2 ± 0.2</td>
</tr>
<tr>
<td>$N_i^{\text{obs}}$</td>
<td>1</td>
<td>0</td>
<td>1</td>
<td>0</td>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>$\mathcal{B}(J/\psi \to \nu \pi)$ Limit</td>
<td>(0.2 ± 0.7 ± 0.5) × 10^{-3}</td>
<td>&lt; 3.9 × 10^{-3}</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

TABLE VII: Expected $\psi(2S) \to \nu \pi$ background yields $N_i^{\text{peak}}$ and $N_i^{\text{bkg}}$, signal efficiencies $\varepsilon_i^{\text{sig}}$, number of observed data events $N_i^{\text{obs}}$, and the resulting branching fraction central value and upper limit at 90% CL, all within the $m_{\pi\pi}$ invariant mass region corresponding to the $\psi(2S)$ mass. Uncertainties are statistical and systematic, respectively. The $N_i^{\text{comb}}$ yields are calculable as $N_i^{\text{bkg}} - N_i^{\text{peak}}$.

<table>
<thead>
<tr>
<th>Channel</th>
<th>$K^+$</th>
<th>$K^0$</th>
<th>$K^{*+} \to K^+\pi^0$</th>
<th>$K^{*+} \to K^0\pi^+$</th>
<th>$K^{*0} \to K^+\pi^-$</th>
<th>$K^{*0} \to K^0\pi^0$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$N_i^{\text{peak}}$</td>
<td>1.4 ± 0.4 ± 0.1</td>
<td>0.6 ± 0.3 ± 0.1</td>
<td>1.4 ± 0.4 ± 0.1</td>
<td>1.0 ± 0.3 ± 0.1</td>
<td>3.5 ± 0.7 ± 0.3</td>
<td>0.6 ± 0.2 ± 0.1</td>
</tr>
<tr>
<td>$N_i^{\text{bkg}}$</td>
<td>1.6 ± 0.4 ± 0.1</td>
<td>0.7 ± 0.3 ± 0.1</td>
<td>1.4 ± 0.4 ± 0.1</td>
<td>1.5 ± 0.4 ± 0.1</td>
<td>3.9 ± 0.7 ± 0.3</td>
<td>0.6 ± 0.2 ± 0.1</td>
</tr>
<tr>
<td>$\varepsilon_i^{\text{sig}} (\times 10^{-8})$</td>
<td>57.2 ± 3.5 ± 3.3</td>
<td>13.1 ± 1.2 ± 1.4</td>
<td>8.1 ± 1.7 ± 0.7</td>
<td>4.9 ± 1.1 ± 0.4</td>
<td>14.2 ± 1.2 ± 1.6</td>
<td>0.6 ± 0.1 ± 0.1</td>
</tr>
<tr>
<td>$N_i^{\text{obs}}$</td>
<td>3</td>
<td>1</td>
<td>1</td>
<td>3</td>
<td>5</td>
<td>1</td>
</tr>
<tr>
<td>$\mathcal{B}(\psi(2S) \to \nu \pi)$ Limit</td>
<td>(5.6 ± 7.4 ± 1.6) × 10^{-3}</td>
<td>&lt; 15.5 × 10^{-3}</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

FIG. 7: (color online) The constraints at 90% CL on $\varepsilon$ and $\eta$ of Eq. (10) for sensitivity to new physics with right-handed currents. The $B \to K\nu\pi$ (diagonal shading) and $B \to K^*\nu\pi$ (grey shading) excluded areas are determined from the upper and lower limits of this $B \to K^{(*)}\nu\pi$ analysis (solid curves) and from the most-stringent upper limits from previous semileptonic-tag analyses $^{12,16}$ (dashed curves). The dot shows the expected SM value.

The combined upper limits for the charmonium branching fraction values are determined to be

$$\frac{\mathcal{B}(J/\psi \to \nu \pi)}{\mathcal{B}(J/\psi \to e^+e^-)} < 6.6 \times 10^{-2}$$

and

$$\frac{\mathcal{B}(\psi(2S) \to \nu \pi)}{\mathcal{B}(\psi(2S) \to e^+e^-)} < 2.0,$$

where $\mathcal{B}(J/\psi \to e^+e^-)$ and $\mathcal{B}(\psi(2S) \to e^+e^-)$ are taken from Ref. $^{31}$. With the addition of a new-physics $U$ boson, these ratios would be proportional to $|f_{e\nu\nu}c_{\chi,\varphi}|$, where $c_{\chi,\varphi}$ and $f_{e\nu\nu}$ are the $U$ couplings to the LDM particles $\chi$ or $\varphi$ and to the $c$-quark respectively $^{13}$. The $J/\psi$ decay ratio yields upper limits at 90% CL of $|f_{e\nu\nu}c_{\chi,\varphi}| < (3.0, 2.1, 1.5) \times 10^{-2}$ for spin-0, Majorana, and Dirac LDM particles respectively. These limits are comparable with those obtained by BES for $J/\psi \to \nu \pi$, in $\psi(2S) \to \pi^+\pi^-J/\psi$ $^{20}$. 

invariant mass regions. The tables also report the combined branching fraction central values and the branchi-
In conclusion, we have searched for the decays $B \to K\nu\bar{\nu}$ and $B \to K^*\nu\bar{\nu}$, as well as $J/\psi \to \nu\bar{\nu}$ and $\psi(2S) \to \nu\bar{\nu}$ via $B \to K^{(*)}J/\psi$ and $B \to K^{(*)}\psi(2S)$, recoiling from a hadronically reconstructed $B$ meson within a data sample of $471 \times 10^6 B\bar{B}$ pairs. We observe no significant signal in any of the channels and obtain upper limits at the 90% CL of $B(B \to K\nu\bar{\nu}) < 3.2 \times 10^{-5}$, $B(B \to K^*\nu\bar{\nu}) < 7.9 \times 10^{-5}$, $B(J/\psi \to \nu\bar{\nu}) < 3.9 \times 10^{-3}$, and $B(\psi(2S) \to \nu\bar{\nu}) < 15.5 \times 10^{-3}$. The branching fraction central values and upper limits are consistent with SM predictions. We report $B \to K^{(*)}\nu\bar{\nu}$ branching fraction limits in Tables VI and VII and $c\bar{c} \to \nu\bar{\nu}$ branching fraction limits in Tables IX and XI. These results include the first lower limit in the $B^+ \to K^+\nu\bar{\nu}$ decay channel, the most stringent published upper limits using the hadronic-tag reconstruction technique in the $B^0 \to K^0\nu\bar{\nu}$, $B^+ \to K^{*+}\nu\bar{\nu}$, and $B^0 \to K^{*0}\nu\bar{\nu}$ channels, and the first upper limit for $\psi(2S) \to \nu\bar{\nu}$. We also present partial branching fraction values for $B \to K^{(*)}\nu\bar{\nu}$ over the full $s_B$ spectrum in Fig. 6 in order to enable additional tests of new-physics models.

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[14] The use of charge conjugate processes is implied throughout this article.